## Rates of exchange and NMR






N -methylformamide (left) and methyl formate (right) in $\mathrm{CDCl}_{3}$ at 90 MHz

## Calculated barriers to rotation



## Rates change as a function of temperature



Variable temperature NMR of DMF

## Slow exchange: integration to determine complex stoichiometry




Integration of methoxy $\left(^{*}\right)$ and adamantane ( $(\bullet)$ signals gave a 4:1 molar ratio.

(Later confirmed by X-ray)

## A Practical Guide - Job plot sample prep

1. Prepare stocks
[A stock] $=5 \mathrm{mM}$
[B stock] $=5 \mathrm{mM}$
2. Create samples with fixed $\left[A_{t}+B_{t}\right]$ as below:

| Tube <br> $\#$ | Vol. A <br> stock <br> $(\mathrm{mL})$ | Vol. B <br> stock <br> $(\mathrm{mL})$ | $\chi_{\mathrm{A}}$ |
| :--- | :--- | :--- | :--- |
| 1 | 0.5 | 0 | 1 |
| 2 | 0.4 | 0.1 | 0.8 |
| 3 | 0.3 | 0.2 | 0.6 |
| 4 | 0.25 | 0.25 | 0.5 |
| 5 | 0.2 | 0.3 | 0.4 |
| 6 | 0.1 | 0.4 | 0.2 |
| 7 | 0 | 0.5 | 0 |

3. Record $\Delta \delta$, calculate $\Delta \delta \bullet \chi_{\mathrm{A}}$, Plot as shown at right


More Examples of Job Plot Data


A


$$
\mathrm{Me}_{4} \mathrm{~N}^{+} \mathrm{I}^{-}
$$

or $\mathrm{Me}_{3} \mathrm{NH}^{+} \mathrm{Cl}^{-}$ B



## Diffusion-Ordered SpectroscopY (DOSY)



Stokes-Einstein relationship:
$D=k T / 6 \pi \eta R_{H}$
D = diffusion coefficient
$k=$ Boltzmann constant
$\eta=$ solvent viscosity
$R_{H}=$ hydrodynamic radius, which can be related to MW by calibration on related molecules

## DOSY for a host-guest complex



A system in fast exchange - real data for $\delta_{\text {free }}$ and $\delta_{\text {bound }}$



1:1 Complex
[peptide] $_{t}=1 \mathrm{mM}$

Hypothetical curves for
$f_{11}$ vs. conc. plots based on the generalized 1:1 binding isotherm


Benesi-Hildebrand Plot


Scatchard Plot


## Exemplary NMR Titration Data



Average $\mathrm{K}_{\text {assoc }}=180 \mathrm{M}^{-1}$

Schalley et al. Chem. Eur. J. 2003, 9, 1332.



## A Practical Guide - Sample preparation

Choose starting concentrations

1. Prepare 5 mL of stock $A$
2. Remove 0.6 mL of stock and put in NMR tube
3. Calculate amount of $B$ needed to make 4 mL of $B$ at $30 \times[A]$
4. Weigh that amount of $B$ into vial, and dissolve in 4 mL of stock $A$
5. Transfer that titrant into a gas-tight 100 or 250 uL syringe

All of this ensures that $A_{t}$ stays constant throughout titration.


## A Practical Guide - Titration

1. Record NMR to determine $\delta_{\text {free }}$
2. Add 10 uL of titrant
3. Record NMR again
4. Repeat...

Hints:
-You want to observe a significant $\Delta \delta$ with each addition. You want lots of data points on the curved part of the isotherm. You want to get as close to saturation as possible. This will require making judgments on the fly and increasing the amount you add as you go along. It is not unusual for the increments to start at 10 uL and to be 250 uL by the end of the titration.

- Mix well at each addition (invert $>5$ times). Mixing is slow in a narrow NMR tube.


## A Practical Guide - Data Analysis

1. In a spreadsheet, record $\delta_{\text {obs }}$ and total volume of titrant added for each spectrum.
2. Convert to the $y$ and $x$ values needed for plotting, $\Delta \delta_{o b s}$ and $B_{t}$.
3. Input these two columns of data into Origin.
4. Fit to the $1: 1$ binding isotherm to determine the parameters $\Delta \delta_{\max }$ and $\mathrm{K}_{\text {assoc }}$. Be sure to try a few different initial guesses. Be sure to check the quality of fit. If you haven't already done so, confirm stoichiometry by Job plot or other method.

## Exemplary Data - van't Hoff Plots


30b

98


Normally 4-5 values for T are enough

Rafaella Faraoni, PhD thesis, ETH Zurich

Host: 30b
Guest: 9-ethyladenine (29)
$[\mathrm{H}]_{\mathrm{l}}=5 \mathrm{mM}$
$[\mathrm{H}]_{0}=5 \mathrm{mM}$
$[\mathrm{G}]_{0}=20 \mathrm{mM}$

$[\mathrm{H}]_{0}=10 \mathrm{mM}$


Solvent: $\mathrm{CDCl}_{3}$ $\mathrm{T}=258-323 \mathrm{~K}$

## Exemplary Data - Very Slow Exchange Kinetics

Exchange of guest $\mathbf{P}$ (complex $\mathbf{1 \cdot P \cdot 1 ; ~ t r i a n g l e s ) ~ f o r ~ g u e s t ~} \mathbf{A}$ (complex $\mathbf{1 \cdot} \mathbf{A \cdot 1}$; squares) was followed over 4 hours taking a new NMR measurement every 5 minutes.




Rebek et al. Proc. Nat. Acad. Sci. USA 1999, 96, 8344.

## NMR Line-Shape Analysis

At a given temperature where intermediate exchange is observed, $k=k_{1}+k_{-1}$ can be determined by fitting:
$A(\omega)=\frac{M_{0} k\left(\Omega_{1}-\Omega_{2}\right)^{2}}{\left(\omega-\Omega_{1}\right)^{2}\left(\omega-\Omega_{2}\right)^{2}+4 k^{2}\left(\omega-\frac{\Omega_{1}+\Omega_{2}}{2}\right)^{2}}$.
$\Omega_{1}=\omega_{\text {obs }}-\omega_{0}$ for signal 1 (offset)
$\Omega_{2}=\omega_{\text {obs }}-\omega_{0}$ for signal 2 (offset)


## Exemplary Data - NMR Line-Shape Analysis



- Red traces are fitted curves, black traces are actual data.


$$
\mathrm{k} \sim 3500 \mathrm{~s}^{-1}
$$

$$
\mathrm{k}=735 \mathrm{~s}^{-1}
$$

$-15^{\circ} \mathrm{C}$


## Exemplary EXSY data for guest exchange



Integrate 3D on-axis peaks and cross peaks to obtain $\mathrm{k}_{1}$ and $\mathrm{k}_{-1}$

See Perrin, C. L.; Dwyer, T. J. Chem. Rev. 1990, 90, 935-967 for a review


