

Practice MT3 (50 marks: 1 minute per mark)

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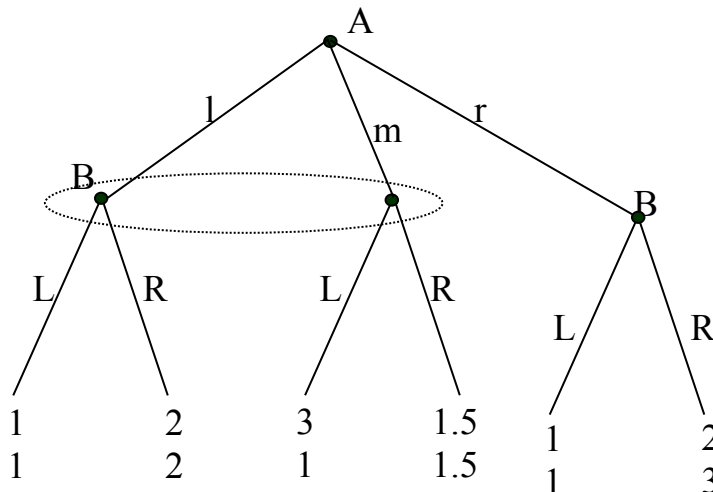
**Question 1** Short-answer questions (10 marks).

- (a) (1) Give two real-world examples of second-degree price discrimination, and (2) two real-world examples of third-degree price discrimination.
- (1) discount vouchers; buy two get the third for free; utility bill with a fixed charge and variable charge; early-bird discounts; etc, etc.
  - (2) charging different prices in different countries; student discounts; UVic tuition for Canadians (low) and international students (high); etc, etc
- (b) Price discrimination is not always possible. List three conditions needed to enable sellers to price discriminate.
- (1) seller needs to have market power
  - (2) It must be permitted by law
  - (3) Arbitrage must be impossible or at least costly
  - (4) for effective price discrimination the seller must know the relevant demand function(s), at least locally

**Notes: (i) Short-answer questions can also be True/False/Uncertain type questions. (ii) the weight on the S-A questions could be varying from say 20% (like in this practice MT) to up to say 40%.**

**Question 2** (10 marks)

Consider the extensive form representation of a game between two politicians, A and B. Politician A moves first and chooses her political position: left (l), middle (m), or right (r). Next politician B decides: left (L) or right (R). The top entry of each payoff vector represents A's payoff, the bottom entry B's payoff



- (a) Consider the following who statements. Tell me whether they are TRUE, FALSE or UNCERTAIN and clarify why in a single sentence.
1. This is a game of imperfect information --> TRUE, B cannot distinguish whether A has chosen "l" or "m"
  2. This is a simultaneous-move game --> FALSE, this is a dynamic game. A chooses before B chooses.
- (b) Give the strategic form representation of the game above. Clarify your notation for the strategies of A and B with an example.

		B			
		Strategies	LL	LR	RL
A	l	(1,1)	(1,1)	(2,2)	(2,2)
	m	(3,1)	(3,1)	(1.5,1.5)	(1.5,1.5)
	r	(1,1)	(2,3)	(1,1)	(2,3)

A's strategies are obvious. As for B's strategies, for example, LR means: "I move L if you moved either l or m and R if you moved r.

**Question 3** (10 marks)

In this question consider the UVic Bookstore, i.e. a monopolist for UVic sweaters with cost function  $C(Q) = 0.5Q^2 + 550$ . Here  $Q$  represents the numbers of sweaters produced and sold.

- (a) (1) Formulate this *monopolist's problem* in case demand were given by  $Q = 90 - P$ . (2) Compute the monopoly price and quantity.
- (1)  $\max_Q \{(90 - Q)Q - 0.5Q^2 - 550\}$  (2) FOC  $90 - 2Q - Q = 0$  Hence it follows that  $Q^* = 30$  and  $P^* = 60$ .
- (b) Show the solution to the monopolist's problem in a graph and indicate the consumer surplus, the producer surplus, and, if any, the deadweight loss.  
 Answer: Notice that  $MR(Q) = 90 - 2Q$ ;  $MC(Q) = Q$ , so upward sloping.  $MR = MC$  at  $Q = 30$ . The welfare maximizing quantity is given by  $P = MC$ , so  $Q = 45$ . Indeed  $MC(45) = 45$ . Graph will now work.

**Question 4** (10 marks)

A monopolist sells in Canada and the US. Canadian demand is given by  $Q_A = 45 - P_A$  and US demand by  $Q_B = 80 - 2P_B$ . Production costs are  $C(Q) = 0.5Q^2$  and assume there are no transportation or border handling costs for the monopolist.

- (a) Compute what are the quantities this monopolist will produce for the Canadian and the US market.
- A: The problem is:  $\max_{Q_A, Q_B} \{(45 - Q_A)Q_A + (40 - 0.5Q_B)Q_B - 0.5(Q_A + Q_B)^2\}$ . The two FOCs are  $45 - 2Q_A - (Q_A + Q_B) = 0$  and  $40 - Q_B - (Q_A + Q_B) = 0$ . Solve

these FOCs to get  $Q_A = 10$  and  $Q_B = 15$ . That is, sell 15 units in Canada and 10 in the US.

- (b) Define what would be meant by *arbitrage* in this context. What assumptions need to be made about the cost of arbitrage in question 4a?

A: In this context, arbitrage would be buying in the US and selling in Canada or the other way around. With  $Q_A = 10$  and  $Q_B = 15$ , we get  $P_A = 35$  and

$P_B = 32.50$ . So the cost of arbitrage must exceed \$2.50 to enable the solution computed in (a)

**Question 5** (5+3+2=10 marks)

A monopolist faces two types of customers. Demand of Type A customers is given by  $Q_A = 50 - P_A$  and demand of Type B customers by  $Q_B = 80 - 2P_B$ . There are equally many of each type of consumer. Assume the monopolist's cost function is given by  $C(Q) = 20Q$ .

- (a) Find the optimal two-part tariff  $T(Q) = F + vQ$  that this monopolist could charge for its products.

The marginal cost is 20 here, so  $v^* = 20$ . If  $v$  were 20 and  $F$  zero, then the CS for A would be  $0.5 \cdot 30 \cdot (50 - 20) = 450$  and that of B would be  $0.5 \cdot 40 \cdot (40 - 20) = 400$ . [use quick graphs if that's helpful!] This shows that the optimal  $F$  is  $F^* = 400$ .

- (b) For the optimal two part tariff you found in (a), what are (1) the deadweight loss, and (2) the consumer surplus of each consumer.

DW loss = 0. There is no deadweight loss (as both consumers buy the efficient quantities b/c the variable fee is set equal to the marginal cost). CS of A is  $450 - 400 = 50$ . That of B is  $400 - 400 = 0$ .

- (c) Give an optimal pricing strategy for this monopolist if perfect price discrimination (= first-degree price discrimination) were possible.

Two part tariffs can do the job here as well. But use two different fixed fees, so charge A the tariff of  $T_A(Q) = 450 + 20Q$ , and B  $T_B(Q) = 400 + 20Q$ . [By the way, notice that this requires you are somehow able to identify who is A and who is B. This was not needed in (a) above. Also, arbitrage should not be possible, or too expensive, but this is also true in (a).]

**This practice MT covered monopoly and game theory pretty well. But it didn't contain a question on oligopoly, while the MT3 of course may have such a question. PS3 had a few good examples.**