Oceanic Isopycnal Slope Spectra: Part II - Turbulence

JODY M. KLYMAK

Scripps Institution of Oceanography, University of California, San Diego, La Jolla CA JAMES N. MOUM

College of Oceanic and Atmospheric Sciences, Oregon State University, Corvallis OR

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ABSTRACT

Isopycnal slope spectra were computed from thermistor data obtained using a microstructure platform towed through turbulence generated by internal tidal motions near the Hawaiian Ridge, and compared to turbulence dissipation rates (ε) estimated using shear probes. The turbulence subrange of isopycnal slope spectra extends to surprisingly large horizontal wavelengths (> 100 m). A four order of magnitude range in turbulence dissipation rates at this site reveals that isopycnal slope spectra $\propto \varepsilon^{2/3} k_x^{1/3}$. The turbulence spectral subrange ($k_x > 0.4$ cpm) responds to the dissipation rate as predicted by the Batchelor model spectrum, both in amplitude and towed vertical coherence (TVC). Scales between 100 and 1000 m are modeled by a linear combination of internal waves and turbulence while, at larger scales, internal waves dominate. The broad bandwidth of the turbulence subrange means that a fit of spectral amplitude to the Batchelor model yields reasonable estimates of ε , even when applied at scales of tens of meters which, in vertical profiles, would be obscured by other finestructure.

1. Introduction

Turbulence in the ocean enhances mixing of tracers and momentum by creating small-scale variance that increases gradients across which molecular diffusion acts. In the ocean's interior, turbulence is usually thought to be the result of breaking small-scale internal waves. Much effort has gone into estimating the rate of turbulence dissipation in the ocean, either by direct measurement (Osborn and Cox 1972), or by characterizing the internal wavefield and assuming that the rate of energy lost from it is a predictable function of its strength (Henyey et al. 1986).

In this paper, isopycnal slope spectra¹ collected in the deep ocean near the Hawaiian Ridge are fit to a simple internal-wave model and the Batchelor spectrum for turbulence (Batchelor 1959). Slope spectra are thought to be dominated by internal waves at low wavenumbers but, since the vertical-to-horizontal aspect ratio of internal waves is small, their influence on horizontal slope spectra does not extend to as high wavenumbers as in vertical strain spectra (Klymak and Moum 2006, hereafter KMI). Conversely, the signature of turbulence extends to

lower wavenumbers in horizontal than to vertical spectra (Fig. 1).

There is a substantial literature describing horizontal temperature spectra in the ocean, much of it overlapping the scales discussed here (McKean and Ewart 1974; Katz 1975; Katz and Briscoe 1979; Marmorino 1987; Dugan et al. 1986). These spectra share many of the characteristics of the spectra sketched in Fig. 1b, slightly red at low wavenumbers and blue at high wavenumbers. The low wavenumbers in these spectra have usually been interpreted as internal waves, and inspired early versions of the empirical spectrum of internal waves (GM75, Garrett and Munk 1975). It was also recognized that the shape and amplitude at high wavenumbers were likely set by turbulence. Patches of high temperature variance have aspect ratios on the order of 100:1 (Rosenblum and Marmorino 1990). Here, similar spectra are related to directly measured turbulence dissipation rates. We also are able to examine the spectra in light of the intervening decades of internal wave and turbulence measurements, predominantly from vertical profilers.

Turbulence is usually measured from specialized vertical profilers (Osborn and Crawford 1980; Moum et al. 1995) or, more infrequently, horizontal towed instruments (Osborn and Lueck 1985; Fleury and Lueck 1992; Moum et al. 2002). Turbulence dissipation rate, ε , can be estimated using shear probes or from dissipation of temperature using fast thermistors. Shear probes are prone to vibration (Moum and Lueck 1985; Levine and Lueck

Corresponding author address: J. Klymak, University of Victoria, Victoria, B.C., jklymak@uvic.ca

¹We cast our spectra in terms of gradients, made in the direction of measurement, of vertical isopycnal displacements, ζ . The vertical gradient, measurable from a vertical profiler, is the vertical *strain* ζ_z . The horizontal gradient, measurable from a towed instrument, is the isopycnal *slope* ζ_x .



FIG. 1. a) Strain spectra with saturated internal-wave subrange and turbulence for four different energy levels and their corresponding turbulence levels assuming $\varepsilon \sim E^2$. After D'Asaro and Lien (2000), except the turbulence is added to the internal-wave spectrum rather than intersecting them with a sharp change of slope. b) Slope spectra in the same wave and turbulence fields. The slope spectra have been computed from the vertical assuming a frequency spectrum with a large M_2 component as described in KMI. (The slightly jagged nature of these spectra is because we represent strain spectra as discrete modes rather than continuous wavenumbers.) This paper is concerned with the high wavenumber portion of the slope spectra (labeled KMII above).

1999), requiring great care in instrument design and deployment. Thus most of this effort has gone into vertical profilers. Thermistors have a finite time constant that attenuates their signal at wavelengths that are relatively low for resolving turbulence (depending on drop speed, Gregg 1999). Internal waves dominate vertical profiles at low wavenumbers. There is a very narrow range of resolved turbulence. More specialized sensors, such as thermocouples, can extend the range to higher wavenumbers (Nash et al. 1999), but these sensors are fragile and do not last long (yet) in oceanic deployments. Estimating turbulence using less-delicate instrumentation would increase our sampling of mixing in the ocean.

There are methods to indirectly estimate turbulence from routine velocity and density measurements. One method is to estimate the strength of the internal wavefield using shear and stratification, then relate it to dissipation rate (Gregg 1989; Polzin et al. 1995; Gregg et al. 2003). This method relies on a fully developed internal-wave spectrum and does not appear to work well in coastal waters and near topography (MacKinnon and Gregg 2003; Kunze et al. 2002; Klymak et al. 2006c). Another approach is to calculate the size of density overturns, and assume that the potential energy in the overturn is dissipated in some fraction of a buoyancy period (Thorpe 1977; Dillon 1982; Moum 1996b). This method works well in highly turbulent flows, but has problems in strongly stratified flows where conductivity-temperaturedensity probes (CTDs) cannot resolve overturns (Klymak and Gregg 2004) and in weak stratification where noise or salinity-spiking induces spurious overturns (Galbraith and Kelley 1996; Johnson and Garrett 2004).

In this paper, the turbulence dissipation rate is esti-

mated directly from temperature spectra obtained using the horizontally towed vehicle MARLINwith the same technology used on vertical profilers. The influence of turbulence extends to much lower wavenumber in slope spectra than in strain spectra (Fig. 1b). One consequence is that estimates of turbulence dissipation rate are more readily made from spectral scaling so that this type of estimate could be obtained with a towed commercial thermistor.

We start with a brief review of the internal-wave and turbulence subranges (section 2), followed by a discussion of MARLINand the experiment site on the Hawaiian Ridge (section 3). The observed spectra are presented in section 4. Next, the high-wavenumber portion of the spectra is fit to turbulence models, and it is shown that the intermediate scales are fit by adding turbulence and internal-wave fits made independently at the extremes of their subranges (section 5). The spectra are fit to determine the turbulence dissipation rate (section 6), and we show that the fit can be done for coarse wavenumbers with equally good effect (section 7). We finish with a short discussion of the possible meaning of adding spectra from two disparate types of motion, and the observation that the turbulence subrange extends to such large horizontal subranges (section 8).

2. Internal-wave and turbulence subranges

The temperature signal is converted to vertical displacements $\zeta = z(T_0) - T$, then taking the first derivative to yield isopycnal-slope ζ_x (KMI). The equivalent quantity from vertical profiles is called the vertical "strain" ζ_z . Displacements remove low-frequency, small-amplitude motions of MARLIN (KMI).

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a. Internal-wave subrange

KMI argues that low wavenumbers are relatively well modeled by

$$\phi_{\zeta_x}(k_x) \approx \phi_0 k_x^{-0.5} \tag{1}$$

where ϕ_0 depends on the stratification, energy level, and frequency content of the internal wavefield. The amplitude, ϕ_0 , is only weakly coupled to the energy level because resolved horizontal wavenumbers are heavily influenced by the saturated part of the wavefield. The power law of the horizontal spectrum, $k_x^{-0.5}$, is a convolution of the linear ($\sim k_z^0$) and saturated ($\sim k_z^{-1}$) subranges (KMI). The two subranges are not distinct in horizontal measurements because of the dispersion relation of a broadband frequency spectrum. We use equation (1) as a model in this paper for simplicity, but emphasize that it does not reflect physics of the wavefield.

b. Turbulence subrange

The turbulence spectrum at high wavenumbers is usually written as a combination of subranges. At the lowest turbulence wavenumbers, the strength of turbulence and the temperature gradient set the level of the displacement spectrum of the *inertial-convective subrange*:

$$\phi_{\zeta_x}^{IC} = 2\pi \chi_{\zeta} C_T \varepsilon^{-1/3} (2\pi k_x)^{1/3} \quad [\text{cpm}^{-1}] \qquad (2)$$

where k_x is the horizontal wavenumber in cycles-permeter, with $C_T \approx 0.4$ (Sreenivasan 1996) and ε is the turbulence dissipation rate. $\chi_{\zeta} = \chi_T (dT_0/dz)^{-2}$ is a scaled version of the dissipation of temperature variance χ_T , where dT_0/dz is the background temperature gradient. At higher wavenumbers, the viscosity of seawater (v) becomes important in the *inertial-diffusive subrange*:

$$\phi_{\zeta_x}^{ID} = 2\pi \chi_{\zeta} q \mathbf{v}^{1/2} \varepsilon^{-1/2} (2\pi k_x), \qquad (3)$$

where $q \approx 2.3$ (Klymak et al. 2006a). In Klymak et al. (2006a), we do not model the spectra with independent subranges, but rather add them to get:

$$\phi_{\zeta_x}^{Turb} = 2\pi \chi_{\zeta} (C_T \varepsilon^{-1/3} (2\pi k_x)^{1/3} + q \nu^{1/2} \varepsilon^{-1/2} (2\pi k_x)).$$
⁽⁴⁾

One consequence of this is that it leads to a lower value of q than usually used. This has a minor effect on the calculations made below.

At the highest wavenumbers there is a viscousdiffusive subrange that is not discussed further here.

In order to relate the spectra to $\epsilon,$ the dependence on χ_ζ is removed as follows. The temperature variance dissipation rate is

$$\chi_T = 2D_T \left\langle (\nabla T)^2 \right\rangle, \tag{5}$$

where D_T is the molecular diffusivity of water and the brackets represent averaging over a homogeneous turbulent patch. Ignoring the lateral and time-dependent terms,

the turbulent equation for temperature variance can be written:

$$D_T \left\langle (\nabla T)^2 \right\rangle = -\langle w'T' \rangle \frac{\partial T}{\partial z}$$
 (6)

$$= K_T \left(\frac{\partial T}{\partial z}\right)^2 \tag{7}$$

where the turbulent temperature flux $\langle w'T' \rangle$ has been cast as a Fickian diffusion working against the mean temperature gradient. These equations can be combined to yield:

$$\chi_T = 2K_T \left(\frac{\partial T}{\partial z}\right)^2.$$
 (8)

If turbulent motions affect buoyancy in the same way they do temperature, $K_{\rho} = K_T$. K_{ρ} is routinely linked to the turbulence dissipation rate and stratification via the Osborn-Cox method:

$$K_{\rho} = \Gamma \frac{\varepsilon}{N^2} \tag{9}$$

where $\Gamma \approx 0.2$ is an empirically defined mixing efficiency (Osborn and Cox 1972; Osborn 1980; Moum 1990, 1996a). This gives:

$$\chi_T = 2 \frac{\Gamma \varepsilon}{N^2} \left(\frac{\partial T}{\partial z}\right)^2. \tag{10}$$

Vertical displacement gradients can be approximated by dividing the spectra by $(dT_0/dz)^2$. Assuming that, on average, $\partial T/\partial z \approx dT_0/dz$, and approximating N^2 by the mean N_0^2 :

$$\chi_{\zeta} = 2 \frac{\Gamma \varepsilon}{N_0^2},\tag{11}$$

].

and rewrite equation (4) as

$$\phi_{\zeta_x}^{Turb}(k_x) = 4\pi \frac{\Gamma \varepsilon}{N_0^2} \left(C_T \varepsilon^{-1/3} (2\pi k_x)^{1/3} + q \mathbf{v}^{1/2} \varepsilon^{-1/2} (2\pi k_x) \right) \quad [\text{cpm}^{-1}]$$
(12)

Using the mean rather than the local gradients is a necessary approximation when using a towed instrument. If N^2 is proportional to $\partial T/\partial z$, as it is in the limited depth ranges considered near Hawaii, then the error in performing the approximation is linear in N^2 . The model will underestimate the spectra where $N_0^2 > N^2$. In the fits performed below, this means that ε will be overestimated in regions of high strain.

c. Intermediate subranges

The wavenumbers between turbulence and internal waves have engendered considerable attention because no appropriate theory exists for the motions there. With horizontal gradient spectra similar to those presented here, McKean and Ewart (1974) note that wavenumbers between internal waves and turbulence had an almost white subrange. McKean (1974) makes a case that the whitening is due to the vertical advection of finescale motions past the instrument. However, his model of turbulence did not include an inertial subrange. The slope of the inertial subrange, $k_x^{1/3}$, is relatively white and accounts for much of the whitening. We will demonstrate below that any remaining whitening of the spectrum at mid-wavenumbers can be accounted for by summing the turbulent and internal-wave spectra:

$$\phi = \phi^{IW} + \phi^{Turb}. \tag{13}$$

3. Instrumentation and experiment site

MARLIN is a towed vehicle, described in Moum et al. (2002); Klymak et al. (2006b), and KMI. A 0.680-inch hydrographic wire deployed from the deck is weighted with a streamlined 1500 kg depressor. MARLIN is attached to the depressor via a 200-m long cable with strain-relief to damp any remaining vibration. MARLIN was ballasted to fly between 20 and 50 m below the depressor. Tow speeds were approximately 1ms^{-1} with variations in the speed and currents inducing small speed and altitude variations in MARLIN, though the cable and depressor damped out ship motions shorter than 20 minutes. MARLIN was equipped with a microstructure suite and conductivity, temperature, and pressure on the nose, and a temperature sensor on a fin that protruded 1.16 m beneath the body (KMI).

The data in this paper was collected from Kauai Channel between Oahu and Kauai as part of the Hawaiian Ocean Mixing Experiment. Our sampling consisted of cross-ridge runs made at approximately 700-m depth, and a dog-leg pattern of runs that approached the ridge, then turned northwest, following the 3000 m isobath (Klymak et al. 2006b). Most of the data presented in this paper was collected near 700 m. At this depth, the mean vertical stratification was $N^2 = 2 \times 10^{-5} \text{ s}^{-2}$, the vertical temperature gradient $dT/dz = 4 \times 10^{-3} \text{ c Cm}^{-1}$ (Fig. 2).

The microstructure suite includes airfoil probes from which estimates of ε are obtained by standard methods (Moum et al. 1995). Contamination of ε measurements by vehicle vibration were diagnosed using accelerometers in the nose of the microstructure package (Levine and Lueck 1999). Vibration signals coherent with the shear-probe signals were removed from the signals and the variance computed to get the dissipation rate. If more than half the variance was removed, the calculated dissipation rate was assumed to be dominated by noise and set to $\varepsilon = 10^{-11}$ m² s⁻³). This biases dissipation averages low, but has minor effect as the signal-to-noise level increases (Moum et al. 2002). For the data discussed here, the noise level was on order $\varepsilon \approx 3 \times 10^{-10}$ m² s⁻³.

4. Isopycnal Slope Spectra

 $\begin{bmatrix} 0 & & & & & \\ 500 & & & & \\ 1000 & & & & \\ 1500 & & & & \\ 2000 & & & & \\ 2500 & & & & \\ 3000 & & & & \\ 10^{-7} 10^{-6} 10^{-5} 10^{-4} & 10^{-4} 10^{-3} 10^{-2} \\ & & N^2 [s^{-2}] & dT/dz [^{0}C m^{-1}] \end{bmatrix}$

FIG. 2. a) Mean stratification profiles for spectra used in this paper. b) Mean temperature gradient profiles. Each dot corresponds to an individual spectra. Profiles were derived from vertical measurements made during the same experiment (Lee et al. 2006).

Isopycnal-slope spectra on wavelengths of 5 km to 0.1 m are presented in the companion paper, KMI. We convert temperature to vertical displacements using the background temperature gradient, and take the derivative in the along-measurement direction to get isopycnal slopes. Binning these spectra turbulence intensity in the record reveals a systematic variation to the spectra (Fig. 3). The 5-km spectra are binned by $K_{\rho} = 0.2\varepsilon/N^2$ which can be considered a dissipation anomaly, where $K_{\rho} = 10^{-5} \text{m}^2 \text{s}^{-1}$ is the open-ocean background. The amplitude of the spectra are normalized by N/N_0 ($N_0 = 5.3 \times 10^{-3} \text{ s}^{-1}$) after the WKB scaling (Katz and Briscoe 1979), though *N* only varies by a factor of 2 for the spectra replotted here (Fig. 2a). Binning demonstrates how the spectra vary with dissipation rate.

At low wavenumbers, the spectra almost collapse. In KMI, we interpret the low wavenumber part of the spectrum as internal waves. At high wavenumbers, the spectra have increasing amplitude with increasing ε . This increase, and a blue slope, extends down to wavenumbers $k_x \leq 10^{-2}$ cpm for all but the weakest turbulence bin.

5. Interpreting turbulence in the presence of internal waves

The averaged isopycnal-slope spectra remain slightly blue, even to wavenumbers $k_x < 10^{-2}$ (Fig. 3). KMI shows that the crossover where the fit to turbulence dominates the internal-wave fit varies inversely with turbulence dissipation rate. This section demonstrates that these motions have spectral shapes and vertical coherence consistent with turbulence. We also show that the shape of spectra between the two types of motion is fit by a linear addition of the models.



FIG. 3. Average isopycnal-slope spectra, binned in one-decade bins of the turbulent diffusivity (as estimated from the shear probes). Spectra have been normalized by their buoyancy frequency for comparison with other studies (though this will not normalize the high wavenumbers). Dashed line is a spectrum from McKean and Ewart (1974, their Fig 2a), collected further offshore at 495 m depth at Hawaii.



FIG. 4. Example spectral fits showing the low and high wavenumber fits. Low wavenumbers are fit only in the region of the spectra in solid black, either $k_x < 10^{-2}$ cpm or to the wavenumbers where the turbulence fit dominates the spectrum; in the last panel the only the lowest two wavenumber bins are fit. The high spectrum is fit from $0.4 < k_x < 4$ cpm.

a. Goodness of fit

A complete model for the slope spectra includes internal wave, inertial-convective, and inertial-diffusive subranges:

$$\tilde{\phi}(\zeta_x) = \phi_0 k_x^{-0.5} + 4\pi \frac{\Gamma \varepsilon}{N_0^2} (C_T \varepsilon^{-1/3} (2\pi k)^{1/3} + q \nu^{1/2} \varepsilon^{-1/2} + q \nu^{1/2} \varepsilon^{-1/2} (2\pi k)^{1/3} + q \nu^{1/2} \varepsilon^{-1/2} + q \nu^{1/2} + q \nu^{1/2} \varepsilon^{-1/2} + q \nu^{1/2} +$$

The internal-wave amplitude ϕ_0 is fit over wavenumbers where there is a distinct red spectrum, or to $k_x = 10^{-2}$ cpm. Three examples show the procedure (Fig. 4) where the low- and high-wavenumber fits are indicated as well as the sum of the two. Turbulent wavenumbers are fit by varying ε to minimize

$$e = \int_{k_0}^{k_+} \left(log 10(\phi^{Turb}/\phi') \right)^2 \mathrm{d}k \tag{15}$$

with $k_0 = 0.4$ and $k_+ = 4$ cpm. The two fits are carried out sequentially, the turbulent fit first, then the internal-wave

fit, since the low wavenumbers are sometimes dominated by turbulence. In neither case are the spectra fit between $10^{-2} < k_x < 0.4$ cpm, outside the range of ambiguity between internal waves and turbulence.

Despite being fit over limited subranges, the model dopes well over intermediate wavenumbers as well (Fig. 4). The logarithmic mean of $\phi/\tilde{\phi}$ as a function of wavenumber, rises slightly and then dips at the lowest wavenumbers, exhibiting some curvature over the turbulence range of the fit (Fig. 5). The average misfits are less than a factor of two, and in most cases are not statistically significant. The dip at intermediate scales ($k_x \approx 10^{-2}$ cpm) may indicate that the turbulence model is too aggressive at these wavenumbers, and turbulence is starting to roll off.

b. Coherence between nose and fin

The shape of the spectra agree well with the model.



FIG. 5. Dissipation-binned spectra divided by the model fit ($\tilde{\phi}$ equation (14)). Shading represents half a standard deviation assuming a log-normal deviation of the ratios. Smoothing of the errors in logarithmic bins of wavenumber space reduces the standard deviations at high wavenumbers. Dashed lines in last panel indicate regions of the respective fits. Note that the low wavenumbers are fit after the high wavenumber model has been subtracted from the spectra. This can mean that the model at the low wavenumbers is entirely dominated by the turbulence. In the last panel this makes the mean misfit drop below unity.

However, being able to match spectral shapes does not necessarily mean signals are governed by the physics associated with each subrange. The coherence between two vertically separated sensors provides additional information. The coherence of signals from the nose on MARLIN and a fin below the nose demonstrate that the coherence is a linear combination of what we are calling "turbulence" with what we are calling "internal waves."

A temperature sensor was installed on the fin 1.16 m below and 1.9 m behind the nose. There were two crossridge tows (approximately 150 km total) at $z \approx 700$ m where the fin thermistor was calibrated and used for coherence estimates. For all the data, the coherence at $k_x = 10^{-3}$ cpm approaches unity (Fig. 6). To compare with theory, the fin sensor was lagged by 1.9 m.

Binning the coherence between the two sensors by ε shows that, as ε increases, the observed coherence between the two sensors rises (Fig. 6). At the lowest dissipation rates, the coherence rolls off at $k_x \approx 3 \times 10^{-3}$ cpm, indicating that the motions have a low aspect ratio. As ε increases, the coherence increases, and for the largest ε the roll-off is near $k_x \approx 4 \times 10^{-2}$ cpm (Fig. 6d). We model this increase of coherence at high wavenum-

We model this increase of coherence at high wavenumbers by calculating the coherence based on modeled spectra of the motion. The coherence between two sensors vertically separated by Δz can be calculated from a model spectrum of the motion $\phi(k_x, k_y, k_z)$ as:

$$\gamma = \frac{\int \int \cos(k_z \Delta z) \phi(k_x, k_y, k_z) dk_y dk_z}{\phi(k_x)}.$$
 (16)

For the motions considered here, $\phi(k_x, k_y, k_z) = \phi^{IW}(k_x, k_y, k_z) + \phi^{Turb}(k_x, k_y, k_z)$. The combined coherence is simply the weighted sum of the coherences of

the components:

$$\gamma = \frac{\gamma^{IW} \phi^{IW} + \gamma^{Turb} \phi^{Turb}}{\phi^{IW} + \phi^{Turb}}.$$
(17)

The procedure for calculating γ^{IW} is given in Katz and Briscoe (1979). For the GM75 model spectrum, γ^{IW} yields the lower thin-dashed lines in Fig. 6. In the bin with the lowest turbulence (Fig. 6a), the observed coherence is consistent with the GM75 coherence, indicating that the motions are dominated by internal waves.

The vertical coherence of the turbulence part of the motion, γ^{Turb} , can be calculated in a similar manner. We could not find a reference for this, so we derive the coherence here. We infer $\phi^{Turb}(k_x, k_y, k_z)$ from the one-dimensional spectrum $\phi_{\zeta}^{Turb}(k_x)$ (equation (12) divided by $(2\pi k_x)^2$) using the assumption that the turbulence is isotropic (Tennekes and Lumley 1972, p. 281):

$$\phi_{Turb}(K) = -\frac{1}{2\pi K} \frac{d}{dK} \phi_{\zeta}(K), \qquad (18)$$

where $K = (k_x^2 + k_y^2 + k_z^2)^{1/2}$. Substituting K for k_x in equation (12) giving:

$$\phi^{Turb}(K) = \frac{4\pi\Gamma\varepsilon}{4\pi^2 N^2} \left(\frac{5}{3}C_T\varepsilon^{-1/3}(2\pi K)^{-11/3} + qv^{1/2}\varepsilon^{-1/2}(2\pi K)^{-3}\right)$$
(19)

We calculate $\gamma^{Turb}(k_x)$ numerically using equation (16) to yield the upper dashed curve in each panel of Fig. 6. The coherence of a turbulent field is higher than the coherence of internal waves at all wavenumbers, and only begins to fall off at $k_x > 0.03$ cpm. When ε is highest, observed coherences (Fig. 6d) are close to the purely turbulent model.



FIG. 6. Towed vertical coherence (squared) between MARLIN's nose and a fin 1.16 m below and 1.9 m behind the nose. Data is averaged in four turbulence bins, and 95% bootstrap confidence intervals are made for each wavenumber. The lower thin-dashed line is the vertical coherence expected from the GM75 spectrum (with bandwidth parameter $j_* = 1$, KMI), the upper thin-dashed line is the coherence expected from homogeneous, isotropic turbulence. The middle thick-dashed line is the coherence expected from a temperature field that is a linear combination of the two types of motion.

The weighted sum of the internal-wave and turbulence coherences is the thick-dashed line of each panel (Fig. 6). We have assumed that ϕ^{IW} remains constant, as indicated by Fig. 3, and increased ϕ^{Turb} in each panel. As ϕ^{Turb} increases, the increase and the shape of the increase in coherence is predicted. The observed coherence tends to be a little higher than the model predicts for all dissipation levels, particularly for the highest dissipation bin.

This calculation assumes a simple addition of turbulence and internal-wave spectra, just as we did above in fitting the shape of the spectra. Neither the fits, nor these coherence calculations, are perfect. However, they explain the leading-order features of the spectra without the need for additional physics and indicate that the signature of turbulence extends to wavenumbers $k_x < 10^{-2}$ cpm.

A caveat is that we have assumed for simplicity that the turbulence spectrum exists and is isotropic at all wavenumbers. However, turbulence is thought to be driven by the overturning of shear or convective instabilities, which have finite vertical extents, so this assumption is not likely to hold at large vertical scales (Gargett 1985). The effect of anisotropy can be estimated by attenuating $\phi^{Turb}(K)$ at large vertical scales (Fig. 7). This is only a crude approximation of anisotropy, but in lieu of a complete theory, we assess the possible effect on our measurements. Attenuating the spectra at a 100-m scale, the coherence is nearly the same as for the fully isotropic case. However, if turbulence is suppressed at smaller scales, the coherence starts to drop significantly. This argues that the coherence from the most turbulent blocks of data (Fig. 6d) consists of turbulence that extends to vertical scales in excess of 100 m. Other work at the study site corroborates the idea that the strongest turbulence is contained in turbulent patches of greater than 100 m in height (Klymak et al. 2006c). Averages from weaker turbulence blocks are not definitive, and could be consistent with the turbulence being suppressed in the vertical at smaller scales.

6. Calculating the dissipation rate from thermistors

In this section we consider how well the dissipation rate can be estimated from the turbulence portion of the temperature spectrum. We consider 32-m long sections of data, yielding approximately 9000 spectra. This scale was chosen as being free of contamination from internal waves for most of the observations (KMI, Fig. 10). Average turbulence dissipation ε was estimated with shear probes over the same intervals to compare with the value estimated from the thermistors (ε_T).

We obtain ε_T as the value of the dissipation that minimizes equation (15) over $0.4 < k_x < 4$ cpm. Again, the cruise-background stratification is used to estimate N^2 . Fitting temperature spectra to obtain ε_T yields encouraging results (Fig. 8). There is considerable spread in the



FIG. 7. Effect on the vertical coherence of 1.16-m separated sensors of attenuating the three-dimensional turbulence in the vertical at the scale indicated for each line. This is a crude approximation to anisotropic turbulence. The dashed line is for no attenuation.

estimates, and individual 32-m blocks of data may make an incorrect estimate by over an order of magnitude but the average results are unbiased. Contributing to the scatter in this comparison is our inability to determine the local value of N^2 , as well as natural geophysical variability.

Spatial binning of ε_T across the ridge shallower than 1000 m demonstrates that the temperature sensors replicate the cross-ridge structure observed with shear probes (Fig. 9). The dissipation estimate from the temperature sensor was first smoothed on a 300 m scale in log-space to remove some of the log-normal variability, equivalent to averaging ten spectra before performing the fit. Both estimates of turbulence dissipation were then binned arithmetically in 5 km bins. There is good agreement across the ridge except on the northernmost edge, where there is not as much data.

As mentioned above, a major drawback of this analysis is not having reliable local values of the stratification N^2 . We could have formed stratification estimates from the fin sensor and another body towed ≈ 40 m above and \approx 200 m in front of MARLINbut the second body was felt to be too far from MARLIN to be useful, and at an aspect ratio that could confuse isopycnal slopes with stratification estimates. The fin was too close to the nose and in turbulent flows was just as likely to be measuring part of an overturn than not. The magnitude of the temperature gradient across any two points in an overturn is likely to be greater than the mean temperature gradient across the whole overturn. The usual approach with vertical profilers is to sort the density first, alleviating this problem, and arriving at a useful measure of stratification but this cannot be done with two point sensors.

The uncertainty in N^2 increases the spread in the distribution between the two estimates. The disagreement



FIG. 8. Comparison of $K_{\rho}^{T} = 0.2\epsilon_{T}N^{-2}$ estimated from 9059 displacement spectra and from the shear probes. a) Twodimensional histogram of the two estimates. The correlation co-efficient between the two estimates is $r = 0.56 \pm 0.01$. b) histogram of the log of the ratios. The log-normal statistics (mean, μ and standard deviation σ of a Gaussian fit) of the log of the ratio are shown.

will also have a bias if there is a correlation between N^2 and ε . There is evidence that lower than normal N^2 increases the likelihood of turbulence in the open ocean (Alford and Pinkel 2000), a result that appears applicable near topography at Hawaii (Levine and Boyd 2005; Aucan et al. 2006; Klymak et al. 2006c). This will bias our temperature-spectra dissipation estimates slightly high (Fig. 9).

We have also assumed that the mixing efficiency, Γ , is a constant. There is evidence that Γ may depend on the buoyancy Reynolds number (Smyth et al. 2001) and thus ε and N^2 , possibly biasing our estimates. This data set is not adequate to test this possibility.

7. Resolution requirements

The ability to see further into the inertial-convective subrange with horizontal tows than vertical profiles opens the possibility of using less-specialized vehicles and sensors to determine turbulence dissipation rates in the ocean. As an example, the temperature probe on a Seabird 9-11 CTD has a noise level of 2×10^{-4} °C at



FIG. 9. Dissipation from the shear probes (gray shading) and from the temperature spectra (line and error bars). Error bars represent bootstrap means in 5-km spatial bins. The crest of the ridge is from approximately 10 to 20 km (see Klymak et al. 2006b).

24 Hz. The frequency response of these sensors is limited by the rate that temperature can diffuse through the protective coating to the thermistor, and attenuates near 8 Hz (Gregg and Meagher 1980). These effects limit the upper wavenumber at which turbulence can be seen with a commercial sensor. As shown here, the lower wavenumber is a function of the relative strength of the internal wave band and turbulence.

We explore the feasibility of using a lower-resolution temperature sensor to fit temperature spectra from a towed vehicle by plotting the isopycnal-slope spectrum for three depths and for a slow (like MARLIN 1 m s⁻¹) and moderate (like SeaSoar, 4 m s^{-1}) tow speed. At the slow tow speed, there is no issue with noise, except for the weakest dissipations at the deepest depths. At faster tow speeds, the wavenumber bandwidth of the measurements is reduced and measurement noise level becomes a factor. However, in much of the ocean large dissipation rates should be detected via this method.

We test this by subsampling our data to represent a more poorly resolved measurement of temperature. Displacement spectra were fit in the wavenumber range $0.04 < k_x < 0.4$ cpm (reducing scales by a factor of 10 compared to our estimates of ε_T). While this would probably not work for weak turbulence at 2000 m and a speed of $U = 4 \text{ m s}^{-1}$, it should be adequate at 700 m. The estimates at these lower wavenumbers are not statistically different from those between $0.4 < k_x < 4$ cpm (Fig. 11).

8. Summary and discussion

This paper describes turbulence temperature spectra from a horizontally towed platform in stratified waters near a site of intense internal-wave generation. These



FIG. 10. Left column: theoretical isopycnal-slope spectra for an instrument towed at 1 ms^{-1} at three different depths (i.e. stratifications and temperature gradients). Right column: tows at 4 ms^{-1} . Dotted lines are the theoretical displacement spectra for four decades of turbulent diffusivity (starting at $K_{\rho} = 3 \times 10^{-6}$). Black lines include an approximate response expected for a temperature sensor with a roll-off at 8 Hz. Dashed lines are the noise floor of an instrument with 2×10^{-4} °C noise at 24 Hz sampling rate.

results are unique because the data was collected in an environment with turbulence levels spanning the highest seen in non-coastal waters to the quiet open ocean. This is also the first time that direct turbulence measurements have been coupled with thermistors for horizontal deepwater tows.

These results have yielded the following insights into isopycnal-slope spectra:

- 1. Horizontal spectra exhibit a turbulence shape $(\phi_{\zeta_x} \sim k_x^{1/3})$ to surprisingly low wavenumbers.
- 2. The subrange between the internal-wave-dominated wavenumbers and the turbulence-dominated wavenumbers is modeled by the linear addition of spectral amplitude.



FIG. 11. As Fig. 8, except the fit to ε_T was made on the displacement spectra for low wavenumbers $0.04 < k_x < 0.4$ cpm, a wavelength well within the range of CTD with a 3-Hz roll-off moving at 4 m s⁻¹. The correlation between the two estimates did not change.

3. ε can be reasonably estimated from these spectra by an inverse of the Osborn-Cox method, even with measurements that can resolve only scales larger than a few meters.

The last observation is useful as an alternate way to estimate turbulence dissipation in the ocean using relatively inexpensive instrumentation. It is important to make the distinction between slope and strain spectra, where internal waves intersect the turbulence spectra at $k_x \approx 1$ cpm (Fig. 1a). Because of the limited wavenumber range of turbulence in the strain spectra, extraction of meaningful estimates of ε is impossible without specialized sensors.

The first two observations bring up interesting questions about the nature of turbulence at large horizontal scales.

a. Why add the spectra?

We have fit the internal-wave and turbulence subranges at wavenumbers where they do not contaminate one another. Simply adding spectral amplitudes fit at these extrema provides a reasonable fit to the spectra at intermediate wavenumbers (Fig. 5). Simple addition of the spectral models also does a good job of predicting the coherence between two vertically separated sensors (Fig. 6). In neither case, however, does the model perfectly fit the data, so it is possible to conceive of other physics than what we have proposed here. However, this additive model has the benefit of simplicity.

We have no a priori justification for adding the spectra in this way. Typically a sharp change between the subranges is used (but also not usually tested). Perhaps a combination of two factors is responsible for the agreement. First, turbulence is observably intermittent over 5 km spectra so, at any given wavenumber, the dominant physics is sometimes turbulence and sometimes internal waves. We have made no attempt to consider homogeneous "patches" of turbulence, primarily because it would be hard to do so and still present internal-wave spectra. Second, there is no reason that "turbulence" cannot co-exist with internal waves. We expect this additive model applies to vertical spectra as well, but the sharper slope of the internal-wave spectra (k_z^{-1}) versus $k_x^{-0.5}$) means the region of overlap is less pronounced. For now, we present the additive model as an observation, and hope that an explanation can be refined from laboratory, numerical, and further fieldwork.

b. Why does the "turbulence" shape extend to such low wavenumbers?

A related issue is the low-wavenumber extent of the turbulence. For the most intense turbulence, there is evidence of a $\phi_{\zeta_x} \sim k_x^{1/3}$ turbulence subrange influencing the spectra to scales exceeding 500 m.

The results in this paper are similar to those of other authors, so we believe that the low-wavenumber extent of the $k^{1/3}$ inertial subrange is not isolated to our measurements. A spectrum from McKean and Ewart (1974, their Fig 2a) is shown in Fig. 3. This spectrum increases and becomes blue at high wavenumbers. Another of their spectra (Fig 2c, their paper) is fit in Fig. 12. Note that the fit is satisfactory at the wavenumbers between the subranges, reducing the need for the additional physics as proposed by McKean (1974).

The results reported by Dugan et al. (1986) are also similar to those presented here (Fig. 13). They measured horizontal temperature spectra in the Sargasso Sea, which they binned by the "intensity" of patches. This yielded spectra that are largely collapsed at low wavenumbers, but have varying levels at wavenumbers $k_x > 2 \times 10^{-2}$ cpm. As they note, the slope in this regime is consistent with an inertial subrange, particularly for the two most turbulent spectra. The results of this paper corroborate these results and verify that increasing "intensity" corresponds to increasing turbulence dissipation levels. Here we estimate the turbulence dissipations from their data, and find very low numbers, consistent with vertical microstructure measurements that also find low dissipation in the Sargasso Sea (Gregg and Sanford 1980). These are further evidence that the inertial sub-



FIG. 12. Fit of the spectrum from McKean and Ewart (1974, their Fig 2c), 500 m (also note that their spectra are half spectra, so we have multiplied by two). The dissipation rate fit to the model is $\varepsilon = 1.9 \times 10^{-9}$ m² s⁻³, or $K_{\rho} = 1.4 \times 10^{-5}$ m²s⁻¹. For this plot $dT/dz = 6 \times 10^{-3}$ °C m⁻¹, and $N = 5.2 \times 10^{-3}$ s⁻¹. The spectrum was digitized from their paper by hand.

range can extend to large horizontal scales. In this case, the largest scales are about 50 m, comparable with the weakest dissipation spectra in Fig. 3, and much larger than any overturns that would be found in such stratified water (even at 1000 times the background dissipation rate the Ozmidov scale is only $L_0 = 0.5$ m).



FIG. 13. Spectra digitized from Dugan et al. (1986, their Fig. 3). Spectra are binned by the authors as "patches of varying intensity." These have been whitened and scaled as in this paper, $dT/dz = 0.11 \text{ }^{\circ}\text{Cm}^{-1}$ and $N = 1.8 \times 10^{-2} \text{ } s^{-1}$. Turbulence subrange was fit for ε (dashed lines), expressed as K_{ρ} . Note the highest values of K_{ρ} here are comparable to the lowest in this paper.

It seems unlikely that motions in our data at $k_x < 10^{-2}$ cpm are isotropic turbulence. The large turbulence patches are probably associated with large breaking waves near the ridge, similar to those found on the flanks (Levine and Boyd 2005; Aucan et al. 2006), but these were not observed to exceed 150 m on top of the ridge at the depths discussed here, and were usually on the order of 50 m (Klymak et al. 2006c). Therefore, the motions at these intermediate wavenumbers are anisotropic.

The horizontal extent of turbulence patches is poorly

understood. Turbulence structures in Hawaii can be observed at a single mooring for a number of hours, and MARLIN is towed through patches of elevated turbulence that are several kilometers long (KMI, Fig. 5), indicating that turbulence patches have a large aspect ratio. Similar results have been observed elsewhere. Itsweire et al. (1989) found 10-m thick layers of unstable Richardson number extending over several kilometers in the upper 100 m of the ocean. Marmorino (1987) discusses a 3-km long patch that has evidence of active turbulence from a temperatures sensor. The aspect ratio of turbulence patches has been argued to be f/N, where f is the Coriolis frequency (Rosenblum and Marmorino 1990). At 700 m at Hawaii f/N = 0.01, so a 10-m thick patch could conceivably be 1 km long. Numerical modeling (Smyth et al. 2001) and oceanic observations (Seim and Gregg 1997; Moum et al. 2003) indicate that turbulence created by Kelvin-Helmholtz billows has a flattened aspect ratio,

We are not aware of numerical or laboratory studies that have ascertained the form for horizontal spectra of turbulence beyond the vertical scale of the patch. Therefore, we have no theoretical explanation for extending the inertial subrange to such large horizontal scales. Most numerical experiments are limited in horizontal extent to contain only one or two overturning scales (Smyth et al. 2001). Numerical work by Riley and deBruynKops (2003) and Lindborg (2006) indicates that turbulence can decay into a continuum of flattened vortices in the horizontal that appear to have a spectral slope similar to those discussed here. This "stratified turbulence" also has vertical gradient spectra power laws of k_z^{-1} , perhaps providing a framework to explain both the turbulence and the "saturated" subranges observed in vertical profiles. Our results indicate that the appropriate shape is a continuation of $\phi_{\zeta_x} \sim k_x^{1/3}$, until either the patch width is reached or the motions are dominated by internal waves. We hope these observations spur further research into the nature of this anisotropic regime.

and it seems reasonable that the same will be true of con-

vective instabilities.

Finally, Holbrook and Fer (2005) note that horizontal spectra computed from traces of seismic reflection transects near the continental rise show that spectra of the reflector displacement have $\phi_{\zeta_x} \sim k_x^{1/3}$ at $k_x < 10^{-2}$ cpm (Fig. 14). A fit to their data predicts a relatively large $K_{\rho} \approx 10^{-3} \text{ m}^2 \text{s}^{-1}$, though this value would fall in the third-highest dissipation bin used above (Fig. 3). The "open ocean" spectrum from their paper (not shown here) does not contain a distinct inertial subrange, but the spectral levels are low enough to suggest $K_{\rho} < 5 \times 10^{-5} \text{ m}^2 \text{s}^{-1}$. The spectrum in Fig. 14 demonstrates a slight dip at $k_x > 2 \times 10^{-2}$ cpm, which cannot be explained by our model, above which there is a noise floor ($\phi_{\zeta_x} \propto k_x^2$). Interpreting seismic data in terms of internal motions is still in its infancy, so the physical meaning of the spectra is still being investigated. However, the seismic results and those reported here, suggest that acoustics



FIG. 14. Near-slope spectrum from (Holbrook and Fer 2005). Data have been plotted assuming traces from their seismic image follow isopycnal displacements, ζ . $N = 3.5 \times 10^{-3} \text{ s}^{-1}$ for the calculations made here. The fit was for $4 \times 10^{-3} < k_x < 2 \times 10^{-2}$.

can possibly be used to remotely estimate strong turbulence dissipation rates.

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Written by J. M. Klymak

mailto:jklymak@uvic.ca

http://web.uvic.ca/ jklymak/WorkTools.html