## **Derivatives & Agriculture**

Lecture Notes

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# Outline



# Markets for Trading Derivatives

Exchange-traded market:

Individuals trade standardized contracts that have been defined by the exchange (e.g., Chicago Mercantile Exchange, International Continental Exchange or ICE in Winnipeg)

Over-the-counter (OTC) market:

Individualized contracts where the market consists of a telephone-and computer-linked network of dealers

Refences: Colin A. Carter, 2003. Futures and Options Markets. (Prentice Hall). John C. Hull, 2012. Options, Futures, and Other Derivatives. 8<sup>th</sup> ed. (Pearson Education).

# **Types of Traders**

**Hedgers** use financial derivatives (such as options) to reduce the risk that they face from potential future movements in a market variable (crop prices, stock values) or even physical variable (weather).

**Speculators** use financial derivatives to bet on the future direction of a market or other variable

**Arbitrageurs** take offsetting positions in two or more financial instruments to lock in a profit.

## Main Types of Derivative Instruments

#### **Common features:**

a contract between two parties for trading something in the future with the terms and price agreed upon today; margin requirements (not for options buyers).

Futures Forwards Options Swaps

#### **Differences:**

**Futures:** contracts are standardized, traded through futures exchanges, subject to daily settlement, guaranteed by a clearinghouse, and has marketability.

**Forwards:** contracts are nonstandardized, traded OTC, and usually settled on the pre-determined date.

**Options:** buyer of an option has right but no obligation while seller has the obligation to deliver when the option is exercised

**Swaps:** usually involves a series of cash flows at a few dates; fixed-floating

## Main Types of Derivatives' Underlying Instruments

| CME Group | TRADING                  | CLEARING | REGULATION |
|-----------|--------------------------|----------|------------|
|           | All Products Home        |          |            |
|           | Featured Products        | Produc   | ct Groups  |
|           | zc Corn                  | Agricul  | tural      |
|           | zs Soybean               | Energy   |            |
|           | CL WTI Crude Oil         | Equity I | ndex       |
|           | NG Henry Hub Natural Gas | FX       |            |
|           | ES E-mini S&P 500        | Interest | t Rates    |
|           | NQ E-mini Nasdaq-100     | Metals   |            |
|           | 6E Euro FX               | Options  | 6          |
|           | GE Eurodollar            | OTC      |            |
|           | ZN 10-Year T-Note        | Real Es  | tate       |
|           | zf 5-Year T-Note         | Weathe   | r          |
|           | GC Gold                  |          |            |

https://www.cmegroup.com/trading/products/#pageNumber=1&sortAsc=false&sortField=oi

## Futures & Forwards

### **Benefits of futures trading**

<u>Hedge risk</u>: Futures trading enables producers to hedge the risks of planting a crop, say, by ensuring the price at harvest time

<u>Enhance price discovery</u>: A commodity firm making a large sale to an overseas buyer can immediately turn around and hedge the sale on a futures market; this transfers information from those who have it to those who do not

<u>Promote storage and enhance efficiency</u>: Prior to futures trading, there were wide swings in agricultural prices; futures trading made storage profitable.



 Futures contracts started with grains and agricultural products and gradually expanded to natural resources (e.g., metals and energy products) and financial futures.  Trading volumes and number of markets have increased rapidly since 1970s. All market data contained within the CME Group website should be considered as a reference only and should not be used as validation against, nor as a complement to, real-time market data feeds.

| Product                 | Code | Contract    |     | Last  | Change | Chart | Open  | High  | Low   | Globex Vol |
|-------------------------|------|-------------|-----|-------|--------|-------|-------|-------|-------|------------|
| Corn Futures            | ZCK9 | MAY<br>2019 | OPT | 365'2 | -0'4   | al    | 365'4 | 366'6 | 365'2 | 5,537      |
| Soybean<br>Futures      | ZSK9 | MAY<br>2019 | OPT | 897'2 | +0'2   | al    | 896'0 | 898'4 | 894'6 | 5,355      |
| Soybean Oil<br>Futures  | ZLK9 | MAY<br>2019 | OPT | 29.87 | -0.12  | a     | 29.99 | 30.04 | 29.85 | 3,673      |
| Soybean<br>Meal Futures | ZMK9 | MAY<br>2019 | OPT | 303.6 | +0.6   | al    | 302.5 | 303.9 | 302.5 | 1,976      |

#### **Futures Contracts for Agriculture**

- Grains and Oilseeds (wheat, corn, soybeans, palm oil, rice, etc.)
- Livestock and meat (cattle, hogs)
- Dairy (milk, butter, cheese)
- Food and fiber (cocoa, coffee, sugar)

https://www.cmegroup.com/trading/agricultural/#featured

| Month                   | Options               | Charts        | Last               | Change            | Prior<br>Settle | Open  | High  | Low   | Volume | Hi /<br>Low<br>Limit | Updated                    |
|-------------------------|-----------------------|---------------|--------------------|-------------------|-----------------|-------|-------|-------|--------|----------------------|----------------------------|
| MAY 2019                | OPT                   | •             | 374'4              | +1'2              | 373'2           | 374'0 | 375'4 | 373'4 | 16,411 | 398'2 /<br>348'2     | 23:31:55 CT<br>17 Mar 2019 |
| JUL 2019                | OPT                   | al            | 383'2              | +1'0              | 382'2           | 383'0 | 384'4 | 382'6 | 6,612  | 407'2 /<br>357'2     | 23:30:26 CT<br>17 Mar 2019 |
| SEP 2019                | OPT                   |               | 389'4              | +0'6              | 388'6           | 389'2 | 390'2 | 389'0 | 2,386  | 413'6 /<br>363'6     | 23:27:53 CT<br>17 Mar 2019 |
| DEC 2019                | OPT                   | al            | 397'0              | +1'0              | 396'0           | 396'2 | 397'4 | 396'0 | 3,862  | 421'0 /<br>371'0     | 23:30:29 CT<br>17 Mar 2019 |
| MAR 2020                | OPT                   | al            | 408'0              | +1'0              | 40 <b>7'0</b>   | 407'0 | 408'2 | 407'0 | 343    | 432'0 /<br>382'0     | 23:14:33 CT<br>17 Mar 2019 |
| MAY 2020                | OPT                   | al            | 412'6              | +0'4              | 412'2           | 412'4 | 413'2 | 412'4 | 31     | 437'2 /<br>387'2     | 21:58:05 CT<br>17 Mar 2019 |
| Corn Fu                 | utures (<br>ww.cmegro | <b>Quotes</b> | 415'6<br>rading/ag | +1'0<br>gricultur | 414'6           | 415'0 | 416'0 | 415'0 | 20     | 439'6 /<br>389'6     | 23:27:53 CT<br>17 Mar 2019 |
| al/grain-ar<br>SEP 2020 | nd-oilseed/           | /corn_quo     | tes_globe<br>-     | ex.html           | 407'0           | -     | -     | -     | 0      | 432'0 /<br>382'0     | 16:00:00 CT<br>17 Mar 2019 |
| DEC 2020                | OPT                   | a             | 409'6              | +0'6              | 409'0           | 409'0 | 409'6 | 409'0 | 27     | 434'0 /<br>384'0     | 19:25:22 CT<br>17 Mar 2019 |
| <b>M</b> AR 2021        | OPT                   | al            | -                  | -                 | 416'4           | -     | _     | -     | 0      | 441'4 /<br>391'4     | 16:00:00 CT<br>17 Mar 2019 |
|                         |                       |               |                    |                   |                 |       |       |       |        |                      |                            |

## **Two Parties of A Futures Contract**

Similar to a spot contract, which is an agreement to buy or sell an asset today, there are two parties to the contract:

- One party assumes a long position, agreeing to buy the underlying asset on a certain specified future date for a certain specified price
- Other party assumes a **short** position, agreeing to sell the asset on the same date for the same price

Long position: holder of the contract is obligated to buy the asset specified in the contract • Pay-off =  $S_T - K$ , where  $S_T$  is spot price of asset at maturity T and K is the 'delivery price' or what the holder of the long contract has to pay for the asset

Short position: holder of contract is obligated to sell the asset specified in the contract

• Pay-off =  $K - S_T$  => if future spot price < the price received by counter-party, the holder loses; otherwise, the holder gains.

## A Simple Example for Payoffs



Long position payoff with K=\$100 at maturity Source: Sacks 2015, p.11-12 Short position payoff with K=\$100 at maturity

Reference: Sacks, J. (2015). *Elementary financial derivatives : a guide to trading and valuation with applications*. Wiley.

## **Offset & Settlement**

Because of the commission costs and the costs of storing and/or transporting commodities, the majority of the futures traders choose to offset their positions by taking an opposite position before the maturity of the contract, instead of taking delivery.

If a futures trader keeps the position open after the expiration date, the settlement can be either in physical form or in cash. Most of futures contracts are settled with a payment, instead of taking possession of the underlying asset.

Johnson, R.S. (2017). Derivatives markets and analysis. John Wiley & Sons, Inc., Hoboken, New Jersey.

### One Key Component for Facilitating Futures Trading -- Clearinghouse (CH)

A corporation that is separate from but associated with a futures exchange

All futures trades are cleared through the CH at the end of the day

Trades must be cleared through a member of the CH, with member paid a commission fee for this service

CH balances books on outstanding futures accounts at the end of each trading day

CH facilitates delivery on futures contracts

### **Illustration of Operation of Clearinghouse**

(Carter 2003, p.70; Johnson 2017, p.8-9)

| Time<br>period | Futures<br>buyer | Futures<br>seller | Contract<br>value | CH position           | Open<br>longs | Open<br>shorts |
|----------------|------------------|-------------------|-------------------|-----------------------|---------------|----------------|
| 1              | А                | В                 | \$19,450          | A's seller, B's buyer | А             | В              |
| 2              | С                | А                 | \$20,700          | C's seller, A's buyer | С             | В              |
| 3              | В                | C                 | \$18,150          | B's seller, C's buyer |               |                |

CH facilities delivery: in essence, the CH becomes each buyer's seller and each seller's buyer.

Suppose A takes a long position on a July corn futures worth \$19,450 (committed to buy 5000 bushels of corn for \$3.89/bu at the settlement date in July), while B takes a short position of the same transaction. It is the CH, however, which has committed to accept delivery from B and to deliver to A.

Suppose the next day, A sells a July corn futures contract to C at \$4.14/bu. Now A's position is closed and the CH pays A (through a broker) a total of \$1,250 (=(4.14-3.89)\*5,000). Meanwhile, because the market moved 'against' B and B's commitment is 'marked to market', at the end of day 2, B receives a 'margin call' and will be required to input \$1,000 into his account (assuming initial and maintenance margins are same).

If C and B liquidate their positions at \$3.63/bu on day 3, how much does C lose and what is B's profit?

## **Options**

### **Background – a few key features**

Traded on exchange and OTC markets

An option gives the buyer the right to do something

Buyer does <u>not</u> have to exercise this right, unlike in a forward or futures contract, where seller (writer) is obligated to buy or sell the underlying asset if the option is exercises.

There is a cost (premium) to acquiring an option, unlike with a forward or futures contract

### **Background – some concepts**

**Call (Put) option**: gives holder of an options contract the right to buy (sell) the underlying asset by a certain date for a certain price

**Strike Price**: the exercise price of the contract

**Expiration Date**: time at which the option is due, or maturity date

For call/put options, buyers are referred to as having **long positions**; sellers are referred to as having **short positions** 

**American** option contracts can be exercised any time up to the expiration date **European** option contracts can only be exercised on the expiration date

### **Background – related to option trading**

**Call** option contracts on 16 stocks started to trade in 1973 on the Chicago Board Options Exchange (CBOE)

**Put** option contracts started trading on CBOE in 1977.

For over-the-counter (**OTC**) options, financial institutions often act as market makers (defined below) for the more commonly traded instruments

Disadvantage of OTC trades is potential **credit risk** – that the contract is not honored

Exchanges have organised themselves to eliminate virtually all credit risk but not **basis risk** -- the value of a derivatives contract does not move in line with that of the underlying exposure

### Background – Market Makers (1)

Exchanges use market makers to facilitate trading. Market maker quotes both a bid and an offer price on an instrument.

In general, bid is a price at which a trader is prepared to buy Similarly, offer (ask) is a price at which a trader is prepared to sell Offer always exceeds the bid with the difference referred to as the bid-offer spread

Exchange sets upper limits for the bid-offer spread. For example, exchange specifies that spread not exceed \$0.25 for options priced at less than \$5; \$0.50 for those priced between \$5 and \$10; \$0.75 for those priced between \$10 and \$20; and \$1 for options priced over \$20)

Market makers make their profits from the bidoffer spread.

| BIDS           | PRICE | OFFERS         |
|----------------|-------|----------------|
|                | 10.19 | Investor       |
|                | 10.08 | Market Maker A |
|                | 10.07 | Investor       |
|                | 10.04 | Market Maker B |
|                | 10.03 | Investor       |
| Market Maker A | 10.01 |                |
| Investor       | 9.99  |                |
| Investor       | 9.98  |                |
| Market Maker B | 9.95  |                |
| Investor       | 9.85  |                |

Fig. 1. Liquid market with investors and market makers, the bid-offer spread is only 2 cents wide & there are a number of buyers & sellers

### Background – Market Makers (2)

#### Source:

http://wildwoodtrading.com/what-ismarket-making/

| BIDS     | PRICE | OFFERS   |
|----------|-------|----------|
|          | 10.19 | Investor |
|          | 10.08 | Investor |
|          | 10.07 | Investor |
|          | 10.04 | Investor |
|          | 10.03 | Investor |
|          | 9.50  | Investor |
|          | 9.42  | Investor |
|          | 9.40  | Investor |
|          | 9.10  | Investor |
| Investor | 8.45  |          |

Fig. 2. Illiquid market without market makers during a large imbalance. There are mostly sellers and a single buyer with a low bid

| BIDS           | PRICE | OFFERS         |
|----------------|-------|----------------|
|                | 9.55  | Market Maker C |
|                | 9.50  | Investor       |
|                | 9.46  | Market Maker B |
|                | 9.45  | Market Maker A |
|                | 9.42  | Investor       |
|                | 9.40  | Investor       |
| Market Maker C | 9.32  |                |
| Market Maker B | 9.30  |                |
| Market Maker A | 9.27  |                |
| Investor       | 8.45  |                |

Fig. 3. Market makers balance and restore liquidity by stepping in to buy the product when other investors do not

### Background – Market Makers (3)

#### EXHIBIT 5: LIQUIDITY PROVIDERS AND THEIR OBLIGATIONS

| Liquidity Provider                       | Description  | Obligations   |
|--|--|---|
| Broker-dealers                           | Broker-dealers facilitating block orders for customers.  | No obligations.   |
| Exchange-<br>registered market<br>makers | Exchange liquidity provider as defined<br>by the rules and liquidity programs<br>established by each exchange.   | <ul> <li>Must be registered on the exchange, maintain adequate capital requirements, and provide continuous two sided quotations.</li> <li>Market makers may have exchange obligations to quote at minimum spreads or sizes for specified proportions of the trading day.</li> <li>Market makers may be required to stand in and facilitate auctions.</li> <li>Compensated by better tiers for fees/rebates, direct payments for providing liquidity, or priority on orders.</li> </ul> |
| Wholesale / OTC<br>market makers         | Market maker that specifically makes markets to smaller regional or retail brokers.  | <ul> <li>Must guarantee client execution but can fulfill this obligation by routing flow out to an exchange instead of committing capital.</li> <li>Generally need to demonstrate and compete on price improvement metrics and execution quality statistics.</li> </ul>   |
| Electronic market<br>makers              | Automated high frequency market<br>makers that seek to capture the bid/offer<br>spread and exchange rebates as a risk<br>premium for providing liquidity.                                  | No obligations.   |
| High Frequency<br>Arbitrageurs           | Proprietary trading firms which employ<br>high frequency trading strategies to<br>conduct statistical or index arbitrage to<br>capture mispricing between correlated<br>or related assets. | No obligations.   |

#### Source: https://seekingalpha.com/article/3588596-market-makers

## An Example of An Option Contract

| KC HBW               | / Wheat O  | ptions   | View Another P                       | Product             | -          | 0   |  |
|----------------------|--|--|--------------------------------------|---------------------|------------|---|--|
| Contrac              | t Specs  | ptiono   | View / Modifer 1                     | Toddot              |            | Procedures  | Open Outcry  |
| Quetes               |  |  | Contract Space                       | Margina             | Calandar   |   | Settlement Team  |
| Futures              | Options Vo   | nume nime & Sales  | Contract Specs                       | margins             | Calendar   | Termination<br>Of Trading   | Trading terminates on the last Friday which precedes by at least two business days the last business<br>day of the month prior to the contract month. Trading in expiring options ceases at the close of the<br>regular CME Globex trading session for the corresponding futures contract. |
| Тур                  | e: American Op   | tions  |                                      |                     |            | Position<br>Limits  | CBOT Position Limits   |
| Contract             | One KC HRW Wh  | eat Futures contract (5,000 bus                                    | hels)                                |                     |            | Exchange<br>Rulebook  | CBOT 14L   |
| Unit                 | 1/8 cent per bush  | el (\$6.25 per contract)   |                                      |                     |            | Block<br>Minimum  | Block Minimum Thresholds   |
| Price<br>Fluctuation | Ion  |  |                                      |                     |            | Price Limit<br>Or Circuit   | Price Limits   |
| Price<br>Quotation   | Cents and eighths  | of a cent per bushel   |                                      |                     |            | Vendor<br>Codes   | Quote Vendor Symbols Listing   |
| Trading<br>Hours     | CME Globex:  | Sunday – Friday, 7:00 p.m<br>Monday – Friday, 8:30 a.m.            | - 7:45 a.m. CT and<br>- 1:20 p.m. CT |                     |            | Strike Price<br>Listing   | Ten (10) cents per bushel for standard options, and five (5) cents per bushel for serial options and for<br>standard options when they become the third listed contract month.   |
|                      | Open Outcry: Monday – Friday, 8:30 a.m. – 1:15 p.m.<br>CT with Post session until 1:20 p.m. CT immediately following the close |  |                                      | e                   | Procedures | Levels of strike price increments: 30 (30 above and 30 below ATM to a minimum strike of 1.00) |  |
| Product<br>Code      | CME Globex: OKE<br>CME ClearPort: K  | E<br>W<br>HP Call: HC  |                                      |                     |            | Exercise<br>Style   | American   |
|                      | Clearing: KW   |  |                                      | ant Mari Int. C     |            | Settlement<br>Method  | Deliverable  |
| Listed<br>Contracts  | December cycle a   | listed for 3 consecutive months<br>ind a second July contract moni | with 6 months in the Ma<br>h.        | irch, May, July, Se | eptember,  | Underlying  | KC HRW Wheat Futures   |

## **Two Parties of An Options Contract**

Same as a futures contract, there are two parties to the contract:  Investor who takes a long position (i.e., agreed to buy option)

 Investor who takes a short position (i.e., has sold or written the option)

Long position: holder of the contract has right (no obligation) to buy (long call) or sell (long put) the asset specified in the contract

- Long call: Payoff =  $max(S_T K, 0)$ , as the option is only exercised if  $S_T > K$ , where  $S_T$  is spot price of asset at maturity T and K is the strike price
- Long short: Payoff=  $max(K S_T, 0)$

Short position: holder of contract is obligated to buy (short put) and sell (short call) the asset specified in the contract

- Short call: Payoff =  $max(K S_T, 0)$
- Short put: Payoff = max( $S_T K$ , 0)

## A Figure for Showing Payoffs with Premium



### Questions

#### **Q1**

Suppose we purchased a \$3.65 July KC wheat put option for 18 cents a bushel via CME. What is the underlying instrument, strike price, premium?

#### **Q2**

To protect against falling prices, should we buy a call or a put option?

### Illustration of Wheat Futures Options: May 17, 2002 WSJ (Carter 2003)

#### Wheat (CBT)

5,000 bu.; cents per bu.

| Price | Jly    | Sep    | Dec    | Jly    | Sep    | Dec               |
|-------|--------|--------|--------|--------|--------|-------------------|
| 260   | 18.500 | 25.250 |        | 2.000  | 4.250  | 4.000             |
| 270   | 11.625 | 18.750 | 28.125 | 5.125  | 7.750  | 7.000             |
| 280   | 6.750  | 13.750 | 22.375 | 10.250 | 12.375 | 11.125            |
| 290   | 4.000  | 10.000 | 17.625 | 17.500 | 18.750 | 16.125            |
| 300   | 2.125  | 7.250  | 14.000 | 25.625 | 25.500 | 22.375            |
| 310   | 1.125  | 5.250  | 11.250 | 34.625 | 33.500 | 29.375            |
|       | <      | Calls  |        |        | Puts   | $\longrightarrow$ |

Buyer of an options contract in wheat can choose strike prices ranging from \$2.60/bu to 3.10/bu. Suppose he chooses to go long on a July wheat options contract at a strike price of 2.80/bu. The premium for this option is  $0.0675/bu \times 5,000$  bu = 337.50, which is paid immediately. If wheat July futures price falls below 2.80/bu, he chooses not to exercise the option, lets the option expire and loses 337.50. If July price exceeds 2.80/bu, he exercises the option and acquires a long position in the futures market. If July price exceeds 2.8675/bu, he will exercise and earn positive net profit. Of course, he can choose to sell a call on a July wheat options contract to offset his position.

## **Option Prices**

# Comprised of two parts:

- Intrinsic value
- Time value

Intrinsic value:

- In the money
- At the money
- Out of the money

Main factors that affecting time value:

- Time to expiration, T
- Volatility of the underlying instrument, σ
- Risk-free interest rate, r
- Intrinsic value
- Dividends that are expected to be paid if applicable

### Questions



If CME May corn futures are trading at \$4.25 and the \$4.00 May corn call option is priced at 50 cents per bushel, what is the premium, intrinsic value and time value?



Suppose you sold a CME \$4.50 July corn call and CME July corn futures fell to \$4.25 on the expiration date, is it possible that you will be required to fulfill the obligation to sell a July corn futures contract?

### **More Questions**

**Q5** 

**Q6** 

If you sell a CME September \$3.90 wheat call option at \$0.6, what is your maximum net loss per bushel in theory?

If what you sell is a put option at \$0.4, what is your maximum net loss per bushel in theory? Suppose a producer purchases a November soybean put option with a strike price of \$4.5 for a premium of \$0.5.

In October, the price of soybean drops to \$4.0 and the premium rises to \$0.8.

The producer offsets his option position and sells his soybean simultaneously (assuming no basis risk and costs). What is her net price?

## Weather Derivatives

- Derivatives are designed based on outcomes of weather indexes, which are not traded in other markets.
- The prime objective is to hedge against volume risk, rather than price risk.



Müller, A., & Grandi, M. (2000). Weather Derivatives: A Risk Management Tool for Weather Sensitive Industries. *The Geneva Papers on Risk and Insurance*. Vol 25. No. 2, 273-287.

## **Types of Weather Indexes**

Temperature is the main underlying weather factor for derivatives.

- Number of days/hours that temperature in certain weeks in late Fall is between −5°C and −8°C → for grapes used in making ice wine
- Heating degree days (HDDs): number of days when temperatures are below 65°F and space heating services are required
- Cooling degree days (CDDs): number of days when temperatures are above 65°F and space cooling services are required
- Growing degree days (GDDs): during growing season, the number of days that temperatures are above 5°C and there is enough heat for crop growth
- Cumulative average temperature (CAT): the cumulative amount of temperature over a period, which can be seasonal or monthly.

# Rainfall, early frosts, hail, snowfall et cetera, can all be used as weather indexes.

### Formulas and An Example

$$HDD = \sum_{d=1}^{D} Max(65 - \overline{T}_{d}, 0)$$
$$CDD = \sum_{d=1}^{D} Max(\overline{T}_{d} - 65, 0)$$
$$GDD = \sum_{d=1}^{D} Max(\overline{T}_{d} - 5, 0)$$
$$CAT = \sum_{d=1}^{D} \overline{T}_{d}$$
$$\overline{T}_{d} = \frac{T_{min} + T_{max}}{2}$$

Note: 18 °C is used as the benchmark in EU

#### **Current Weather**



RH: 28% Wind: S 8 mph Pressure: 1013 mb

| Day  | Hi                | Low                        | Average | Weather | HDD        | \$Impact |  |  |  |
|------|-------------------|----------------------------|---------|---------|------------|----------|--|--|--|
| тни  | <b>54°</b>        | <b>34°</b>                 | 44      |         | 21°        | \$420    |  |  |  |
| FRI  | <b>52°</b>        | 37°                        | 45      |         | <b>20°</b> | \$400    |  |  |  |
| SAT  | <mark>52°</mark>  | <b>37°</b>                 | 45      |         | <b>20°</b> | \$400    |  |  |  |
| SUN  | <b>56°</b>        | 37°                        | 47      |         | 18°        | \$360    |  |  |  |
| MON  | <b>54°</b>        | 37°                        | 46      |         | 19°        | \$380    |  |  |  |
| TUES | <mark>58</mark> ° | 37°                        | 48      |         | 17°        | \$340    |  |  |  |
| WED  | <mark>61</mark> ° | 30°                        | 46      |         | 19°        | \$380    |  |  |  |
|      |                   | Total \$2680/ per contract |         |         |            |          |  |  |  |

Source: https://www.investopedia.com/trading/market-futures-introduction-to-weather-derivatives/

## Payoffs

A call option can be claimed when the value of the weather index is above a specified strike value, while a put option can be claimed when the value of the weather index is below a specified value

$$p(w)_{put} = \begin{cases} \lambda(K_1 - w), & \text{if } w \le K_1 \\ 0, & \text{if } w > K_1 \end{cases}$$
$$p(w)_{call} = \begin{cases} 0, & \text{if } w < K_2 \\ \lambda(w - K_2), & \text{if } w \ge K_2 \end{cases}$$

where p(w) is the payoff;  $\lambda$  is the tick size (dollar value per unit of the weather index);  $K_1$  and  $K_2$  are the strike values, respectively; and w is the weather index.

## Where to Buy Weather Derivatives



## The Beginning of Weather Derivatives

1997: First weather transactions (OTC) took place between Enron and Koch Industries, based upon some temperature indices to compensate the energy producer in case of a mild winter

1999: Trading in weather derivatives began on the Chicago Mercantile Exchange (CME), with HDDs

1998: First European deals took place between Enron and Scottish Hydro Electric on a similar basis

### Some Key Dates on CME



However, many derivative products could not draw enough traders and were unlisted. Now CME offers HDD and CDD contracts for 8 American cities (Las Vegas, Atlanta, Chicago, Cincinnati, New York, Dallas, Minneapolis, Sacramento); HDD and CAT contracts for 2 European cities (London, Amsterdam).



HDD call options can be used to protect against the negative impacts from <u>cold or warm</u> winter on business.

Beverage or ice-cream industry can use CDD <u>call</u> <u>or put</u> options to hedge the risk of cool summer.

Examples:

https://www.cmegroup.com/education/articles-and-reports/weather-options-overview.html

## **Pricing Weather Derivatives**

The premium (price of option) is calculated from the expected payoff:

$$c = \mathrm{e}^{-r(T-t)} Ep$$

where *c* is the premium, *r* is a risk-free periodic market interest rate, *t* is the date the contract is issued, *T* is the date the contract is claimed, and *Ep* is the expected payoff:

$$Ep = \int_{0}^{\infty} p(w) f(w) dw$$

where f(w) is the probability density function of the weather index w, p(w) is the payoff, and the integral is from 0 to  $\infty$ because w cannot take on negative values.

## **Modelling Weather Variables**

#### Two methods

- Time series (econometrics)
- Stochastic processes (simulation)

Daily Temperatures

### • Two aspects

- Frequency
   (2 state Markov chain)
- Magnitude (distribution)

Daily Precipitation

