

Agricultural Economics and Policy: Practical #3B

February 11, 2016

Given the following information for a 1500 ac farm, construct a linear programming model that determines how much of each crop to plant.

| Crop | Observed Acreage (ac) | Average Yield (bu/ac) | Price (\$/bu) | Average costs (\$/ac) |
|--------|-----------------------------|-----------------------------|------------------|-----------------------------|
| Wheat | 500 | 42 | \$7.50 | \$192.0 |
| Barley | 200 | 70 | \$4.25 | \$169.5 |
| Canola | 450 | 38 | \$11.50 | \$229.0 |
| Peas | 250 | 45 | \$6.75 | \$163.8 |
| Oats | 100 | 110 | \$2.75 | \$152.50 |

1. Solve the following simple model using GAMS:

$$\text{Maximize} \quad R = \sum_{k=1}^n (p_k x_k y_k - c_k x_k)$$

$$\text{Subject to} \quad \sum_{k=1}^n x_k \leq 1500$$

$$x_k \geq 0$$

2. Now include the following constraint and solve the problem again:

$$x_k \leq x_k^{obs} + 0.01, \forall k$$

For these constraints find the associated shadow prices, λ_k , and use this information to modify the objective function above assuming a quadratic cost function: $c_k = a x_k + \frac{1}{2} b x_k^2$. Then:

$$b_k = 2 \times \lambda_k / x_k^{obs} \text{ and } a_k = c_k - \frac{1}{2} \times b_k \times x_k^{obs}$$

Use the cost function in place of $c_k x_k$ in the objective function, so the revised objective is:

$$\text{Maximize} \quad R = \sum_{k=1}^n (p_k x_k y_k - a_k x_k - \frac{1}{2} b_k x_k^2)$$

Solve the revised problem using GAMS.