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Another look at the income elasticity of non-point source air pollutants: a semiparametric approach

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Abstract

In this paper, a semiparametric model is used to examine the relationship between pollution and income for three non-point source pollutants. Statistical tests reject the quadratic specification in favor of the semiparametric model in all cases. However, the results do not support the inverted-U hypothesis for the pollution–income relationship.

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JEL classification: C13; Q40; Q25

1. Introduction

The environmental Kuznets curve (EKC) hypothesis suggests an inverted-U relationship between economic growth and environmental degradation. The most common test of this hypothesis has been to regress measures of ambient air and water quality on various specifications of per capita income and other relevant regressors, generally using a quadratic or cubic functional form. Dasgupta et al. (2002) express concern about the appropriateness of functional forms in the empirical literature: “in most cases, the implied relationship between income growth and pollution is sensitive to inclusion of higher-order polynomial terms in per capita income whose significance varies widely”. Our purpose is to investigate the issue of functional form, using the same data as Khanna (2002). Employing US data for 1990, Khanna uses a quadratic specification, regressing the logarithm of the ambient concentration of a pollutant on logarithm

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of income and a number of control variables. Including a quadratic term in income implies that the relationship is constrained to be U-shaped or an inverted U shape, thus disallowing the possibility of two turning points, say. To address this, we revisit her results using a nonparametric approach to estimation.

To the best of our knowledge, only three papers in the EKC literature (Giles and Mosk, 2003; Taskin and Zaim, 2000; Millimet et al., 2002) have used purely nonparametric models, but none have used a semiparametric model. Since Khanna's preferred model for each of the three pollutants has at least 22 regressors, pure nonparametric estimation is not feasible (due to the curse of dimensionality). Also, given that her dependent variable is based on different numbers of observations, the implied heteroskedasticity in the model has to be properly taken into account by appropriately adjusting the standard semiparametric estimation technique. We also test Khanna's parametric specification against our semiparametric model using a test by Li and Wang (1998).

2. Econometric model

The semiparametric model employed here is given as:

$$y_i = m(x_i) + z_i' \delta + u_i, \quad i = 1, \dots, n \quad (1)$$

where y_i is the logarithm of ambient concentration of a particular pollutant in region i ; x_i is the logarithm of median household income in region i ; z_i is a $p \times 1$ vector of demographic, political, and other control variables; u_i is the random error term with $E(u_i|x_i, z_i) = 0$. Khanna's (2002) model is a special case of Eq. (1) with $m(x_i) = \beta_1 x_i + \beta_2 x_i^2$. We estimate Eq. (1) for carbon monoxide (CO), ozone (O₃) and nitrogen oxides (NO_x), but unlike Khanna, we use a nonparametric approach.

While Khanna uses weighted least squares approach with the number of observations at each site as the weights, we modify the standard nonparametric estimation of model (1) to take into account the heteroskedasticity. Following Robinson (1988), Stock (1989), and Kniesner and Li (2002), we estimate $f(x_i)$ (the density function of x_i), and the conditional means, $E(y_i|x_i)$ and $E(z_i|x_i)$ by $\hat{f}_i = \frac{1}{nh} \sum_{j=1}^n K_{ij}$, $\hat{y}_i = \frac{1}{nh} \sum_{j=1}^n y_j K_{ij} / \hat{f}_i$, and $\hat{z}_{ik} = \frac{1}{nh} \sum_{j=1}^n z_{jk} K_{ij} / \hat{f}_i$, respectively, where $K_{ij} = (K(x_i - x_j)/h)$ is the kernel function (we used a normal kernel), z_{ik} is the k th component of the z_i vector, and h is the smoothing parameter.¹ Our density weighted, heteroskedasticity adjusted estimator of δ is given as $\hat{\delta} = S_{(z-\hat{z})\hat{f}}^{-1} S_{(z-\hat{z})\hat{f}, (y-\hat{y})\hat{f}}$ where $S_{A\hat{f}, B\hat{f}} = n^{-1} \sum_{i=1}^n w_i A_i \hat{f}_i w_i B_i' \hat{f}_i$, $S_{A\hat{f}} = S_{A\hat{f}, A\hat{f}}$, and w_i is the square root of the number of observations for the i th region.

To obtain estimators of $m(x_i)$ and its derivative (which denotes the income elasticity of pollution), we first rewrite model (1) as: $y_i - z_i' \hat{\delta} = m(x_i) + v_i$, where $v_i = z_i' (\delta - \hat{\delta}) + u_i$ is the new error term.

Then, using a Taylor series expansion, this equation can be rewritten as:

$$y_i - z_i' \hat{\delta} = m(x) + (x_i - x)\beta(x) + \text{error} \quad (2)$$

where $\beta(x)$ is the first derivative of $m(x_i)$ evaluated at $x_i = x$.

¹ We used $h = c \cdot \text{std}x \cdot n^{-1/5}$ where $\text{std}x$ is the standard deviation of the variable x , and we used $c = 0.8, 1, 1.2, \text{ and } 1.4$. Since the results were very similar across the c values, to save space we present the results for $c = 1$. The results for all c values can be obtained from the authors upon request.

Table 1

Comparison of parametric and semiparametric environmental kuznets curve model estimates, carbon monoxide, ozone and nitrous oxides

Explanatory variables	CO model				Ozone model				NO _x model			
	1	2	3	SP	1	2	3	SP	1	2	3	SP
Income	-0.108**	-1.261	23.838		0.021	-0.537	0.805		0.004	-4.689*	16.585	
Income squared	(0.053)	0.059	-2.489		(0.512)	(0.367)	(0.931)		(0.952)	(0.000)	(0.442)	
Income cubed		(0.247)	(0.144)			(0.348)	(0.909)			(0.000)	(0.397)	
			0.086				0.004				0.071	
			(0.134)				(0.886)				(0.323)	
Population density	0.155*	0.156*	0.156*	0.182*	0.016*	0.016*	0.016*	0.013*	0.120*	0.121*	0.121*	0.104*
	(0.000)	(0.000)	(0.000)	(0.000)	(0.004)	(0.005)	(0.005)	(0.020)	(0.000)	(0.000)	(0.000)	(0.000)
% Minorities	0.042**	0.043*	0.040**	0.052*	0.026*	0.026*	0.026*	0.034*	0.088*	0.084*	0.082*	0.079*
	(0.051)	(0.048)	(0.063)	(0.016)	(0.008)	(0.009)	(0.009)	(0.001)	(0.000)	(0.000)	(0.001)	(0.000)
% Unemployed	-0.047	-0.047	-0.047	-0.040	-0.006	-0.004	-0.004	-0.025	-0.004	-0.016	-0.017	-0.026
	(0.218)	(0.218)	(0.221)	(0.305)	(0.777)	(0.841)	(0.837)	(0.268)	(0.933)	(0.765)	(0.751)	(0.614)
% Labor in manufacturing	0.055	0.068**	0.071**	0.142*	0.030**	0.035**	0.035**	0.029	0.109*	0.162*	0.172*	0.242*
	(0.132)	(0.076)	(0.063)	(0.000)	(0.100)	(0.068)	(0.068)	(0.148)	(0.015)	(0.000)	(0.000)	(0.000)
% with high school	-0.055	-0.044	-0.037	-0.054	-0.017	-0.010	-0.010	-0.003	0.008	0.057	0.057	-0.017
	(0.211)	(0.331)	(0.418)	(0.333)	(0.476)	(0.686)	(0.696)	(0.918)	(0.89)	(0.323)	(0.326)	(0.803)
% of voters registered	0.226**	0.227**	0.225**	0.442*	-0.058	-0.059	-0.059	-0.043	-0.581*	-0.639*	-0.628*	-0.681*
	(0.059)	(0.058)	(0.059)	(0.000)	(0.222)	(0.215)	(0.217)	(0.356)	(0.000)	(0.000)	(0.000)	(0.000)
% of houses rented	0.054	0.067	0.068	0.063	-0.017	-0.011	-0.01	-0.021	0.037	0.072	0.075	0.050
	(0.213)	(0.135)	(0.130)	(0.179)	(0.378)	(0.586)	(0.597)	(0.340)	(0.470)	(0.155)	(0.138)	(0.314)
% Female headed households	-0.033	-0.029	-0.03	-0.087*	-0.008	-0.007	-0.007	-0.017	-0.122*	-0.120*	-0.121*	-0.125*
	(0.230)	(0.291)	(0.279)	(0.007)	(0.646)	(0.697)	(0.689)	(0.390)	(0.001)	(0.001)	(0.001)	(0.001)
Urban dummy	0.310*	0.303*	0.301*	0.262*	0.009	0.007	0.007	0.018	0.260*	0.256*	0.259*	0.320*
	(0.000)	(0.000)	(0.000)	(0.000)	(0.704)	(0.770)	(0.769)	(0.456)	(0.000)	(0.000)	(0.000)	(0.000)
Adjusted R ²	0.47	0.471	0.472		0.314	0.314	0.313		0.769	0.779	0.779	
Number of observations	509	509	509	509	820	820	820	820	305	305	305	305

p-values are provided in parentheses.

*Indicates statistical significance at the 5% level or better.

**Indicates statistical significance at the 10% level or better.

Nonparametric kernel estimators of $m(x)$ and $\beta(x)$ can be obtained by using a generalized form of the local linear least squares estimation approach. In particular, we minimize the objective function $(y - Z\hat{\delta} - X_\gamma(x))' \sqrt{K(x)}\Omega^{-1}\sqrt{K(x)}(y - Z\hat{\delta} - X_\gamma(x))$ with respect to $m(x)$ and $\beta(x)$, where y is a $n \times 1$ vector, Z is a $n \times k$ matrix, X is a $n \times 2$ matrix with $X_i = [1(x_i - x)]$ as a typical element, $\gamma(x) = [m(x)\beta(x)]'$ is a 2×1 vector, $\sqrt{K(x)}$ is a $n \times n$ diagonal matrix with the square root of the kernel function K_{ij} as a typical element, and Ω^{-1} is the inverse of an $n \times n$ diagonal matrix with w_i as the i th diagonal element. The resulting estimator of $\gamma(x)$ is given as: $\hat{\gamma}(x) = \{X' \sqrt{K(x)}\Omega^{-1} \sqrt{K(x)}X\}^{-1} \{X' \sqrt{K(x)}\Omega^{-1} \sqrt{K(x)}(y - Z\hat{\delta})\}$.

For more details about the generalized local linear estimator but in the context of panel data models, see Henderson and Ullah (2003).

3. Results

So that the results are comparable, the variables in z_i in model (1) are the same as in Khanna (2002) and are provided in Table 1. All of the variables in Table 1 are in logarithmic form, except the dummy variable indicating whether or not the region is urban (=1). We include but do not report the results for nine dummy variables for EPA regions, and two to three (depending on the pollutant) dummy variables to account for highly influential observations, exactly as in Khanna (2002).

We first estimated parametric specifications of model (1) with $m(x_i) = \beta_1 x_i$, and then $m(x_i) = \beta_1 x_i + \beta_2 x_i^2 + \beta_3 x_i^3$ to see how sensitive Khanna's specification is to alternative functional forms. The results are given in Table 1 along with Khanna's result. Note that, for both CO and NO_x , the statistical significance of the income variable is highly sensitive to specification of functional form. For example, in the CO model, income is a statistically significant for the linear specification but not for the quadratic and cubic specifications; on the other hand, for NO_x , the income variable is

Table 2
Distribution of income elasticities of pollutants

Item	CO		Ozone		NO _x	
	SP	Khanna	SP	Khanna	SP	Khanna
Mean	-0.069	-0.081	0.020	0.037	0.088	0.064
Standard deviation	0.211	0.066	0.160	0.014	0.300	0.225
Minimum	-0.916	-0.256	-0.583	0.033	-0.535	-0.720
Percentile distribution						
10th	-0.319	-0.176	-0.068	0.036	-0.350	-0.237
20th	-0.286	-0.141	-0.049	0.039	-0.271	-0.132
30th	-0.224	-0.112	-0.020	0.042	-0.152	-0.020
40th	-0.139	-0.086	0.013	0.044	0.093	0.047
50th	-0.062	-0.070	0.052	0.049	0.171	0.099
60th	0.016	-0.055	0.103	0.052	0.242	0.131
70th	0.087	-0.042	0.132	0.056	0.301	0.190
80th	0.125	-0.025	0.142	0.061	0.343	0.244
90th	0.175	-0.006	0.215	0.070	0.359	0.326
Maximum (100th)	1.649	0.089	0.853	0.106	1.319	0.644

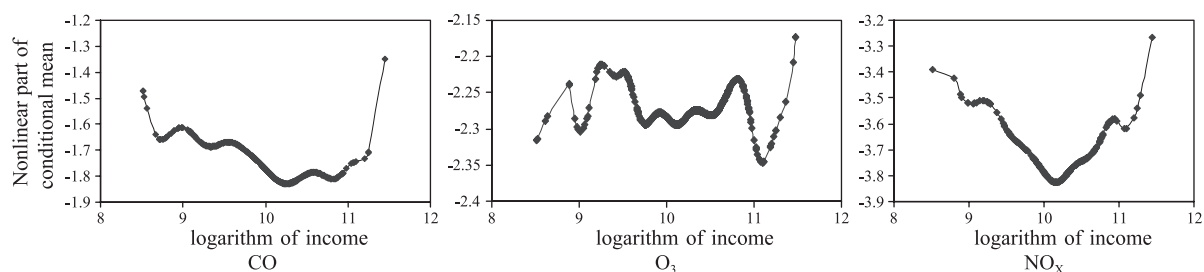


Fig. 1. Concentration of pollutant versus income.

statistically significant for the quadratic specification but not for the others. Therefore, our preferred model is the semiparametric model that does not impose any functional form restriction on the income variable. We also tested Khanna's quadratic specification against the semiparametric alternative using Li and Wang's (1998) test. For $c=1$, the values of the test statistic for CO, O₃ and NO_x are 166.471, 10.883, and 89.111, respectively, with the bootstrapped critical values at 1% level of significance being 1.257, 1.205 and 1.334, respectively. The null hypothesis that the quadratic specification is appropriate is clearly rejected in each case. The results are not sensitive to the choice of c .

In Table 2, we provide various distributional statistics for the semiparametric income elasticity estimates, $\hat{\beta}(x_i)$ for $i=1, \dots, n$ for each pollutant, and for the elasticity estimates from Khanna's parametric model (denoted k).² While the mean values are similar across the two models, the percentile distributions indicate that the elasticity estimates are quite different.

Plots of the estimates of the nonlinear components of the logarithm of income (vertical axis) for CO, O₃ and NO are provided in Fig. 1 for $c=1$. The results agree with Khanna's conclusion that none of the plots exhibit an inverted-U relationship between the pollutant concentration and income.

4. Conclusion

In this paper, we use a semiparametric framework to extend the work of Khanna (2002) to study the relationship between three pollutant concentrations and income using US data. The advantage of the nonparametric approach adopted here is that it allows the data to determine the functional form with respect to the income variable, rather than imposing an ad hoc functional form a priori. This approach is useful in avoiding the problem of functional form misspecification.

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² The results for the other c values are available from the authors upon request.

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