

Example # 2: insurance with adverse selection (Campbell, ch 3.10)

issue: when individuals apply for insurance, insurer cannot identify likelihood of loss

- health
- attitude towards driving

does this unobservable heterogeneity explain some properties of insurance policies? - in particular, combinations of deductible and cost?

Set-up:

Two types of individuals; differ in *exogenously det'd*

risk: indexed by π ; high risk is π_h ; low risk π_l

(Note: ranking as in general case, with π instead of θ)

Assume: individuals are risk averse in income

Market: consider competitive market (rather than monopoly)

- profits = 0 will drive results

Who's what? Principal = planner

Agents = individual demanders of insurance

Benchmark: first best insurance

consider single individual:

- probability of accident is π ; price p is exogenous (market determined); utility is $U(w)$
 - value of w depends on state (accident or not) and amount of insurance
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- State 1: accident; consumption is wealth= x : a if no insurance, $a+c$ if has insurance.
 - State 2: no accident; consumption is $w=y$: z if no insurance purchased, $z-pc$ if has insurance;

Ind'l's expected utility: $EU = \pi u(x) + (1 - \pi)u(y)$
without insurance, $EU = \pi u(a) + (1 - \pi)u(z)$
if buy insurance, $EU = \pi U(a+c) + (1-\pi)U(z-pc)$

In state space, slope of iso-EU curve is

$$\frac{dC_2}{dC_1} = -\frac{\pi U'(x)}{(1-\pi)U'(y)}$$

$= -\pi / (1 - \pi)$ where $y = x$, along
certainty line

*Ind'l with higher risk, who has $\pi_h > \pi_l$, will have
steeper IC

What about the budget line the individual faces?

- depends on cost of insurance, p
- if individuals are identical
- on representative policy,

$$\text{Exp profits} = -\pi c + (1-\pi)pc$$

- how will this change as coverage changes?
- competitive industry: zero expected profits on the avg policy: Implies $p = \frac{\pi}{(1-\pi)}$
- if $p > \frac{\pi}{(1-\pi)}$, expected profits are strictly positive.
- then individual's budget line: for any state contingent wealth pairs,

$$Ew = \pi x + (1-\pi)y = \pi(a+c) + (1-\pi)(z - pc)$$

- holding wealth constant

$$dEw = \pi dx + (1-\pi)dy = \pi dx + \frac{\pi}{p}dy = 0$$

$$\text{So slope of budget line is } -p = -\frac{\pi}{1-\pi}$$

This equals slope of iso-EU along certainty line
Hence: optimal choice of insurance, if *fair*
insurance (that is, with zero expected profits)- full
insurance: consumer moves to certainty line.

So: benchmark equilibrium?

Both types of consumers purchase full insurance.
Cost depends on type: high risk consumers pay more than low risk consumers:

$$p_l = \frac{\pi_l}{(1-\pi_l)} < \frac{\pi_h}{(1-\pi_h)} = p_h$$

So if no accident, high risk consumers have lower wealth; full insurance equates wealth across states, so high risk consumers have lower EU=realized U.

Private information on risk

Are 1st best contract feasible? No: high risk ind'l has incentive to misrepresent, to lower price & raise U.

Since high risk ind'l must be paid to reveal true risk, in eq'm with adverse info this ind'l will receive higher EU.

Low risk individuals will choose a contract which

1. gives them higher EU than being taken as high risk (and paying higher price)
2. satisfies self- selection constraint for high risk

Result: high risk get full insurance, higher price
low risk take less-than-full insurance: lower price and deductible.
firms? still competitive, still make Eprofits=0